

Dynamic characterisation of Össur Flex-Run Prosthetic feet for a more informed prescription

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1 **Dynamic characterisation of Össur Flex-Run Prosthetic feet for a more**
2 **informed prescription**

3
4 **Abstract**

5 *Background:* The current method of prescribing composite Energy Storing and
6 Returning (ESR) feet is subjective and is based only on the amputee's static body
7 weight/mass.

8 *Objectives:* The aim is to investigate their unique design features through identifying
9 and analysing their dynamic characteristics, utilising modal analysis, to determine
10 their mode shapes, natural damping and natural frequencies. Full understanding of
11 the dynamic characteristics can inform on how to tune a foot to match an amputee's
12 gait and body condition.

13 *Methods:* This paper presents the modal analysis results of the full range of Össur
14 Flex-Run running feet that are commercially available (1LO-9LO).

15 *Results:* It is shown that both the undamped natural frequency and stiffness increase
16 linearly from the lowest to highest stiffness category of foot. The effect of over-load
17 and under-loading on natural frequencies is also presented. The damping factor for
18 each foot has been experimentally determined and it was found to be ranging
19 between 1.5-2.0%. An analysis of the mode shapes also showed a unique design
20 feature of these feet that is hypothesised to enhance their performance.

21 *Conclusions:* A better understanding of the feet dynamic characteristics can help to
22 tune the feet to the user's requirements.

23 (194 words)

24
25 **Clinical relevance**

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3 26 This information is needed in order to better predict how the dynamic data can
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5 27 influence the gait pattern and symmetric transition from walking to running. The data
6
7 28 is needed to better understand the role dynamic characteristics of the foot plays
8
9 29 when prescribing the prosthesis for walking or running.

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12 30 (48 words)

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15
16 32 **Keywords:** damping, dynamic characteristics, modal analysis, mode shape, natural
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18 33 frequency, prosthesis, energy-storing and returning.

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22 35 **Background**

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25 36 Sport prostheses are used by both upper- and lower-limb amputees while
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27 37 participating in sports and other physical activities. With advances in medicine and
28
29 38 an emphasis on maintaining physical fitness, the population of athletes with
30
31 39 impairments is growing and receiving great attention ^{1, 2}. This has revealed a
32
33 40 considerable shift in the way our culture considers disabilities over the last few
34
35 41 decades ^{3, 4}. Until the 1980s most prosthetic feet were designed with the main
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37 42 objective of restoring basic walking ability and simple occupational tasks ⁵. The need
38
39 43 for higher performing feet made has led designers to utilise lightweight and more
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41 44 advanced materials such as Carbon Fibre Reinforced Plastic Composite (CFRP).
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43 45 This has resulted in the development of a new generation of energy-storing-and-
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45 46 returning (ESR) feet, with unique shape and geometrical features. The ESR
46
47 47 transforms Potential Energy (PE), into strain energy and returns it back into the body
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49 48 mass in the form of Kinetic Energy (KE) in a short impulses thus helping amputee to
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51 49 accelerate in a forward motion ⁶. Their introduction has changed the nature of
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3 50 amputee sprinting sport. ESR feet are now available in many categories, in terms of
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5 51 their stiffness/performance, catering for most types of recreational activity.
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8 52 The energy efficiency of ESR feet varies between different suppliers. Their
9
10 53 energy return rates have been found to range from 31% ⁷ to as high as 95% ^{6, 8}.
11
12 54 Studies of the biological/intact lower-limb have found that the ankle can generate a
13
14 55 241% energy return ⁷. Hence, an ESR foot falls a long way short of replacing the
15
16 56 mechanical performance of the biological limb. Closer examination of the dynamics
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18 57 of ESR feet identifies several parameters that are capable of affecting the
19
20 58 performance of amputee runners when using these feet. This includes the original
21
22 59 shape, the length of the foot, the overall dynamic elastic response to impulse
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24 60 synchronisation and metabolic cost.
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28 61 By definition the dynamic characteristics of ESR feet are their natural
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30 62 frequency, mode shapes and damping factors ⁹⁻¹¹. Although running with ESR feet is
31
32 63 an impulse driven action, the natural frequency of the spring-mass system plays an
33
34 64 important role to facilitate the transition from vibration to impulse. Other factors
35
36 65 affecting performance of runners using ESR feet could be the excessive metabolic
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38 66 cost, specially due to lack of gait symmetry as observed in unilateral amputees ¹².
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40 67 The effect of each factor needs to be studied individually and their influence on
41
42 68 motion can then be better understood.
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46 69 Over the years, debates of fairness of lower-limb prosthesis running
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48 70 technology in sport were raised ¹³⁻¹⁵. To address this issue, research to investigate
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50 71 static and dynamic characteristics of various prosthetic feet have been carried out.
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52 72 Lehmann et al. conducted studies to evaluate the biomechanical and metabolic
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54 73 performance differences between two different prosthetic foot designs ¹⁶. This study
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56 74 used SACH (Solid-Ankle Cushion-Heal) prosthetic feet to test for dynamic elastic
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3 75 response. It was found that the natural frequencies of oscillation for the prosthetic
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5 76 feet were too high to provide energy storage and release that could be synchronised
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7 77 with the kinematic requirements. This finding is not unexpected as the feet used for
8
9 78 this test were not designed to store and release a large amount of strain energy such
10
11 79 as those made by Össur (Flex-Run) or Blatchford (BladeXT). Noroozi et al.
12
13 80 investigated the link between gait symmetry and the effect of dynamic elastic
14
15 81 response of the ESR foot to impulse in unilateral and bilateral amputees ¹⁷. Noroozi
16
17 82 et al. hypothesised that human input impulse, is needed in order to compensate for
18
19 83 loss of energy in one step. This impulse can only assist the motion if it's applied at
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21 84 the right moment and with a force trajectory that closely maps onto the foot. This
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23 85 phenomenon could potentially enhance performance if the foot is used at its
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25 86 optimum dynamic characteristics.
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30 87 The effect of lack of symmetry due to dissimilar stiffness's on energy transfer
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32 88 rate was investigated by Aslani et al. ¹². It was demonstrated that energy
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34 89 consumption due to lack of gait symmetry is higher than that in symmetric gait and
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36 90 will cause severe fatigue over longer running durations, such as in 200 or 400 metre
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38 91 sprints. It can be shown that an able-bodied individual having a symmetric gait uses
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40 92 less energy than a unilateral amputee when walking ¹⁸⁻²⁰. Oudenhoven et al. also
41
42 93 indicated that the stiffness of the prosthesis is an important parameter to optimize
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44 94 running performance. With this information, the athletes can regulate the leg stiffness
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46 95 during distance running at their preferred step frequencies ²¹. These findings infer
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48 96 running efficiency/improved performance can be gained if the running gait can be
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50 97 made symmetrical. Therefore, knowledge of the dynamic characteristics of such feet
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52 98 is important to assist in developing a symmetrical running gait.
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3 99 This paper presents the modal analysis results of nine stiffness categories of
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5 100 Össur Flex-Run ESR feet in order to understand their dynamic characteristics
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7 101 (natural frequencies, damping and mode shapes). The effect of over-load and under-
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10 102 loading of the ESR foot on the natural frequencies is also presented.

11
12 103 The findings presented in this paper are of importance as the data is not
13
14 104 currently available elsewhere. The data is needed to better understand the role
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16 105 dynamic characteristics of the foot plays when prescribing the prosthesis for walking
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18 106 or running.

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22 23 108 **Methods**

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25 109 The experimental procedure and methodology used to determine the natural
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27 110 frequencies, mode shapes and damping factor of the Össur feet is discussed in this
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29 111 section.

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33 34 113 *Össur Flex-Run*

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36 114 The Flex-Run is described as featuring a long toe lever and efficient energy return
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38 115 (<https://www.ossur.com/prosthetic-solutions/products/sport-solutions/flex-run>). The
39
40 116 full length keel/toe lever is designed to match the length of the sound foot to provide
41
42 117 improved support to the prosthetic limb during late stance. It is claimed that the users
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44 118 spend equal time on the prosthetic foot and natural limb to provide improved walking
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46 119 dynamics and reduced impact to the sound limb. This could lead to improved walking
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48 120 symmetry and reduced impact to the sound limb. Meanwhile, vertical forces
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50 121 generated at heel contact are stored and translated into a linear motion described as
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52 122 Active Tibia Progression. This action is designed to reduce the need to actively push
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123 the body forward using the contralateral foot and also equalizes stride length. The
 124 benefit of this could be a more natural gait and reduced walking effort.

125 The Flex-Run is offered in a range of stiffness values, divided into specified
 126 categories and are prescribed according to the mass of the amputee through the
 127 stiffness prescription guide from Össur (Table 1). It should be noted, that little or no
 128 consideration for the specific ability or desired activity level of the amputee is taken
 129 into account in the prescription guide.

130

131 Table 1: Flex Run stiffness prescription guide

High to Extreme Impact Level	Weight kg	Weight lbs.
1LO	37-44	81-96
2LO	45-52	97-115
3LO	53-59	116-130
4LO	60-68	131-150
5LO	69-77	151-170
6LO	78-88	171-194
7LO	89-100	195-220
8LO	101-116	221-256
9LO	117-130	257-287

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133 Due to the distinct difference in the stiffness of the feet, they will be
 134 distinguished by their rating names assigned by the manufacturer as 1LO-9LO
 135 (Figure 1).

136 Figure 1: Full range of Flex-Run Categories.

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138 *Modal Analysis*

139 Modal analysis is a well-established experimental method for identifying modal
 140 parameters (frequency, mode shapes and damping) in any static elastic
 141 structure/system. The technique used to extract these parameters is called

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3 142 Experimental Modal Analysis (EMA) [21, 22]. The test structure is artificially excited
4
5 143 by using either an impact hammer, or one or more shakers. A force transducer is
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7 144 used to measure the input excitation force to the system while the output response of
8
9 145 the system is normally measured by using accelerometers. Input and output
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11 146 vibration signals of several locations of the system are determined to obtain a
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13 147 discrete number of Frequency Response Functions (FRFs). Then, the FRF obtained
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15 148 undergoes curve fitting to extract the modal frequencies, modal damping and residue
16
17 149 mode shape of the system [23, 24].
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21 150 Complete modal analysis investigations were conducted on nine Össur ESR
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23 151 feet. A mass of 53kg was attached to each of the nine feet and a full modal analysis
24
25 152 was conducted for every foot-mass system combination. In each case, the masses
26
27 153 were secured in such a way that the line of action of the total weight passed through
28
29 154 the ground reaction point of the foot creating a balanced/equilibrium condition
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31 155 (Figure 2). The fixings were approximately 120 degrees apart and each had enough
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33 156 slack to ensure the displacements in all three orthogonal directions were not
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35 157 suppressed.
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41 159 Figure 2: Experimental set-up of free-free modal testing.
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45 161 A total of 18 discrete locations were selected on each foot to attach the
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47 162 accelerometers (Figure 3). The Impulsive excitation technique was used as the test
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49 163 method throughout the study to determine the elastic and damping properties of the
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51 164 feet²². An impact hammer, tri-axial accelerometer, in-house data acquisition system
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53 165 and modal analysis software were used to investigate the dynamic characteristics.
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55 166 The specification of the instrumentation used can be found in Table 2. The input
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3 167 signal was the excitation force from the manual impact hammer whereas the output
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5 168 signal was the response due to impact measured by the accelerometer. A data
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7 169 acquisition (DAQ) system consisting of National Instrument NI-USB-9234 modules
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9 170 controlled by the DASyLab software was used. A manual impact hammer was
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11 171 connected to channel 1 of the National Instrument (NI) dynamic analyzer and a tri-
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13 172 axial accelerometer was connected to channel 2, 3 and 4 respectively. In this
14
15 173 experiment, a roving tri-axial accelerometer was used while manual impact hammer
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17 174 was excited at fixed degrees of freedom, i.e., point 13 and 2 in the x-axis and z-axis
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19 175 respectively. The tri-axial accelerometer was roved from point 1 to point 18
20
21 176 measuring the response of the structure in the x, y and z directions and this gave a
22
23 177 single-input, single-output (SISO) analysis. A sampling rate of 2048 samples/sec
24
25 178 was used, and the vibration signal was collected for 2 seconds, so a total of 4096
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27 179 samples were recorded for post-processing. The modal analysis software (ME'Scope
28
29 180 software) was used to draw the three-dimensional structural model of the test rig in
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31 181 coordinate points where every point was connected by straight lines as shown in
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33 182 Figure 3. The displayed point numbers represented each discrete location as in the
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35 183 actual ESR foot.

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40 184 Furthermore, the FRF estimations acquired through DASyLab software were
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42 185 post-processed by using Me'Scope software. A polynomial curve fitting method was
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44 186 used in the software to extract the modal parameters. Thus, the mode shape
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46 187 obtained corresponding to each vibration mode was recorded and animated using
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48 188 the wire mesh model drawn. Modal damping, 2σ is approximately equal to the width
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50 189 of the resonance peak at 70.7 % of the FRF peak magnitude value, which is the
51
52 190 same as half of the peak magnitude value squared. Hence, 2σ is the width at the half
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54 191 power point of a resonance peak in the unit of rad/s or Hz.
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Figure 3: Wire-mesh model of Flex-Run used for modal analysis

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195 Table 2: Detailed instrumentation characteristics

INSTRUMENTS	DESCRIPTION
1LO-9LO Flex-Run feet	Used as test rig to perform modal analysis
PCB Impact Hammer, Model 086C03	Sensitivity: 2.25 mv/N Tip type: medium tip with vinyl cover Hammer mass: 0.16kg Frequency range: 8kHz Amplitude range: ± 2200 N peak
PCB ICP Accelerometer, Model 356B18	Sensitivity: 1000mv/g Frequency range: ($\pm 5\%$) 0.5 to 3000 Hz Amplitude range: ± 5 g peak
NI USB Dynamics Signal Acquisition Module, Model NI- USB 9234	Number of channels: 4 ADC resolution: 24 bits Type of ADC: Delta sigma (with analog pre- filtering)
DASYLab v10	Sampling rate: 2048 samples/sec Block Size: 4096 Channel 1: Impact hammer Channel 2: Accelerometer x-axis Channel 3: Accelerometer y-axis Channel 4: Accelerometer z-axis Averaging: 5 for static conditions Windowing: Force for excitation signal Exponential for response signal
ME'Scope v6.0	To process collected data from NI-DASYLab To define the structural geometry for frequency response function (FRF) modal Analysis To determine the natural frequencies, damping and animated mode shapes after curve fitting process

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Using the damped natural frequency and damping obtained from modal

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analysis, the undamped natural frequency can be calculated from the damped

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natural frequency (equation 1).

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$$\omega_d = \omega_o \sqrt{1 - \zeta^2} \quad (\text{eq. 1})$$

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203 where, ω_d = damped natural frequency (rad/s), ω_o = undamped natural frequency
 204 (rad/s) and ζ = damping ratio.

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206 By using the constant mass of 53kg and the undamped natural frequency, the
 207 stiffness of each foot can be determined (equation 2).

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$$\omega_o = \sqrt{\frac{k}{m}} \quad (\text{eq. 2})$$

210

211 where, k = stiffness (N/m), m = mass (Kg)

212

213 Results

214 Table 3 presents the natural frequencies and damping of 1LO-9LO feet with fixed
 215 53kg mass system. The results show that the system possesses the same natural
 216 frequency when excited by knocks in X and Z direction. This implies all excitations in
 217 these two directions will always excite this natural. This is close to the natural
 218 frequency of the running gait for most athletes which has been shown in previous
 219 research to reach 4.31Hz during sprinting [25].

220

221 Table 3: Dynamic characteristics of 1LO-9LO feet with fixed 53kg mass

Flex-run	1 st Natural Frequency knocked in X-dir (Hz)	Damping (%)	1 st Natural Frequency knocked in Z-dir (Hz)	Damping (%)
1LO	3.94	1.55	3.90	1.93

2LO	4.02	1.66	4.04	2.06
3LO	4.13	1.65	4.14	1.54
4LO	4.24	1.61	4.24	1.73
5LO	4.64	1.43	4.64	1.63
6LO	4.87	1.65	4.78	1.88
7LO	5.04	1.77	5.00	1.84
8LO	5.21	1.8	5.22	1.81
9LO	5.29	1.54	5.33	1.69

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Table 4 presents the undamped natural frequency and the stiffness of each foot using equations 1 and 2. The results show that both the undamped natural frequency and stiffness of the feet increase from the lowest stiffness category (1LO) to the highest stiffness category (9LO).

Table 4: Dynamic characteristics of 1LO-9LO based on fixed 53kg mass

Flex-run	Damped natural frequency (Hz)	Damping (%)	Undamped natural frequency (Hz)	Stiffness (N/m)
1LO	3.920	1.740	3.921	32161.72
2LO	4.030	1.860	4.031	33993.51
3LO	4.135	1.595	4.136	35784.68
4LO	4.240	1.670	4.241	37626.04
5LO	4.640	1.530	4.641	45058.14
6LO	4.825	1.765	4.826	48726.54
7LO	5.020	1.805	5.021	52745.4
8LO	5.215	1.805	5.216	56922.73
9LO	5.310	1.615	5.311	59011.67

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Figure 4 shows that with the stiffness of 1LO-9LO known, and assuming the boundary condition is fixed, natural frequency can be predicted based on different mass or masses to be used on a specific foot due to the linearity of the data.

Figure 4: Plot of a) undamped natural frequency (Hz) and b) Stiffness (N/m) against ESR foot stiffness category.

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3 237 The results show that by simple adjustment of the stiffness when used with
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5 238 the same body mass, the natural frequency can be controlled. Noroozi et al.
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7 239 described the behaviour of the mass and foot system to be similar to a trampoline ⁹.
8
9 240 ¹¹. If the frequency of the bouncing action during running matches the natural
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11 241 frequency of the perceived mass/spring system then the mass will vibrate. This
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13 242 cyclic rhythm is a form of energy input into the system that is needed to maintain this
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15 243 steady state cyclic/periodic motion, by replacing the loss of energy in one cycle due
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17 244 to damping.
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21 245 Damping is an important factor in this study. Damping data is not readily
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23 246 available for ESR feet. The decay rate has been used to predict the drop in
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25 247 amplitude of the vibration per unit time. Using the decay rate makes it possible to
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27 248 calculate the percentage drop in amplitude with respect to time elapsed. The
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29 249 damping characteristic for a given system must be physically measured as it cannot
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31 250 be determined using simulation tools. The damping characteristic of the feet have
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33 251 been experimentally determined and the damping of the first bending mode was
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35 252 found to range between 1.5-2.0%. This low damping reduces the energy dissipation
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37 253 in one cycle and thus less energy input into the system is required to maintain the
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39 254 steady state cyclic motion before take-off from the ground.
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43 255 These modal test results also show the mode shape that is most relevant or
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45 256 suitable for the running action (Figure 5). The mode shapes of all Flex-Run feet are
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47 257 supplied separately as Supplemental Digital Content. It was noticed during this
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49 258 investigation that the Flex-Run tested possessed a unique geometrical characteristic
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51 259 that initiates or promotes a natural and perpetual forward leaping response when
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53 260 excited as its natural frequency. The recoil motion during bounce gave the system a
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55 261 perpetual forwards motion even without any forward excitation force. This important
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3 262 phenomenon, known as Active Tibia Progression by Össur, could reduce the need to
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5 263 actively push the body forward to have a more natural gait and also reduces the
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7 264 walking effort. Without further testing it can only be hypothesised that this could be
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10 265 due to the special geometrical features of these Össur feet, where energy could be
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12 266 stored in the foot in one direction and released naturally in a different direction that is
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14 267 usually aligned with the direction of the run. In a bilateral amputee this can have
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16 268 another significant effect, which is steady-state symmetric beat frequency that can
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18 269 enhance performance over longer distance runs. Further study of this phenomenon
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21 270 will be the subject of future publications.
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272 Figure 5: First bending mode of 1LO at 3.94Hz and 3.90Hz with free-free boundary
273 condition knocked in X&Z-direction respectively
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275 Discussion

276 Although modal analysis is a powerful tool it is highly sensitive to the influence of
277 other parameters such as changes in boundary conditions that can affect the
278 dynamic response to excitation. This is a very important issue as in a free-free modal
279 testing, the change of boundary condition during modal testing changes due to foot
280 flexure and alignment which will result in discrepancies in the dynamic
281 characteristics obtained. This also implies that using these feet with anything other
282 than strings to hold them in position, such as dedicated test rigs will result in modal
283 data that are not representation of the foot and mass system in isolation. That is
284 because dissimilar material rigs with much higher stiffness will substantially change
285 the boundary condition and the results will show the natural frequencies of the test
286 rig instead of the foot and mass system.

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3 287 This paper indirectly demonstrates the dynamic flexibility of CFRP composite
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5 288 materials for application in advanced dynamic systems. Specific detail regarding the
6
7 289 individual constituents of the material and its construction are unknown. However,
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10 290 the composite laminates used to manufacture running specific feet are all
11
12 291 unidirectional and woven carbon pre-impregnated epoxy. The laminate lay ups are
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14 292 non-symmetric and uses a specific laminate lay up for each foot category. Laminates
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16 293 are autoclaved cured and then machined to size.
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20 21 295 **Conclusion**

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23 296 Nine Össur Flex-Run feet, constituting the full range of feet that are commercially
24
25 297 available (i.e. 1LO-9LO), were investigated and the dynamic characteristic results
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27 298 are presented. Currently no such data is available regarding these feet and the
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29 299 influence of mass, stiffness and natural frequency is not properly understood.

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32 300 This paper presents the damping, mode shapes and natural frequencies of all
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34 301 of these feet. This information will be needed in order to better predict how the
35
36 302 dynamic data can influence the gait pattern and symmetric transition from walking to
37
38 303 running. From the first bending mode shape, it was noticed during this investigation
39
40 304 that the Flex-Run possessed a unique geometrical characteristic that initiates or
41
42 305 promotes a natural and perpetual forward leaping response without any forward
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44 306 excitation force when excited as its natural frequency. Further study of this
45
46 307 phenomenon is warranted.
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6
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11 316 **Author contribution**

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14 317 All authors contributed equally in the preparation of this manuscript
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18 319 **Declaration of conflicting interests**

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21 320 The authors declare that there is no conflict of interest.
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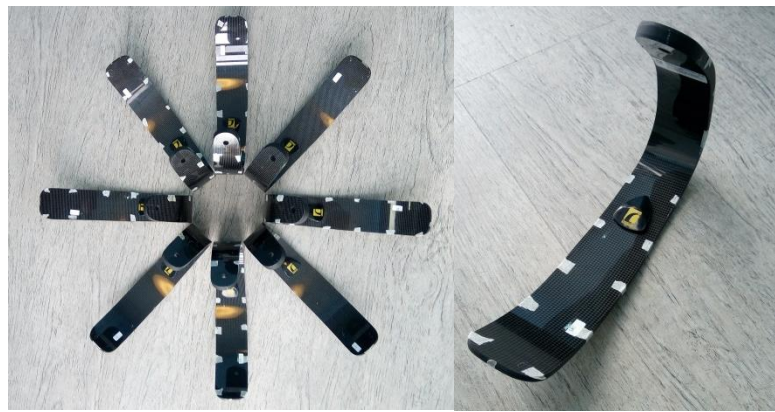


Figure 1: Full range of Flex-Run™

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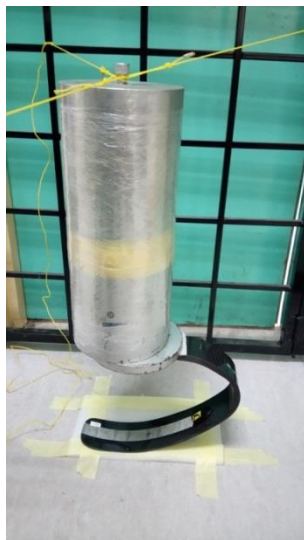


Figure 2: Experimental set-up of free-free modal testing

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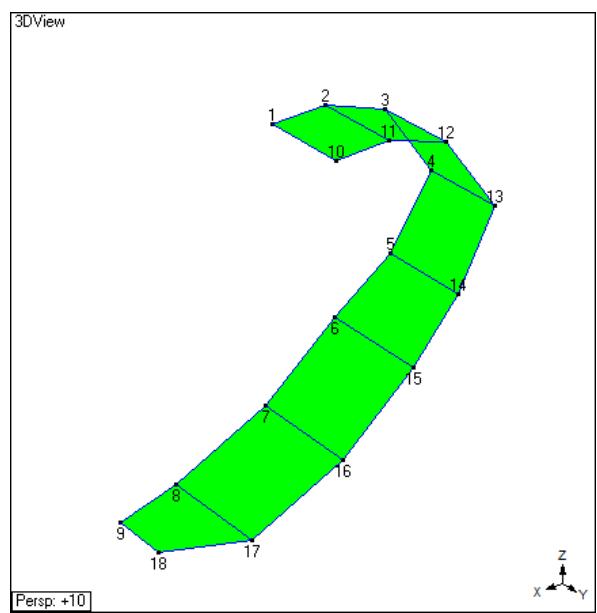


Figure 3: Wire-mesh model of Flex-Run™ used for modal analysis

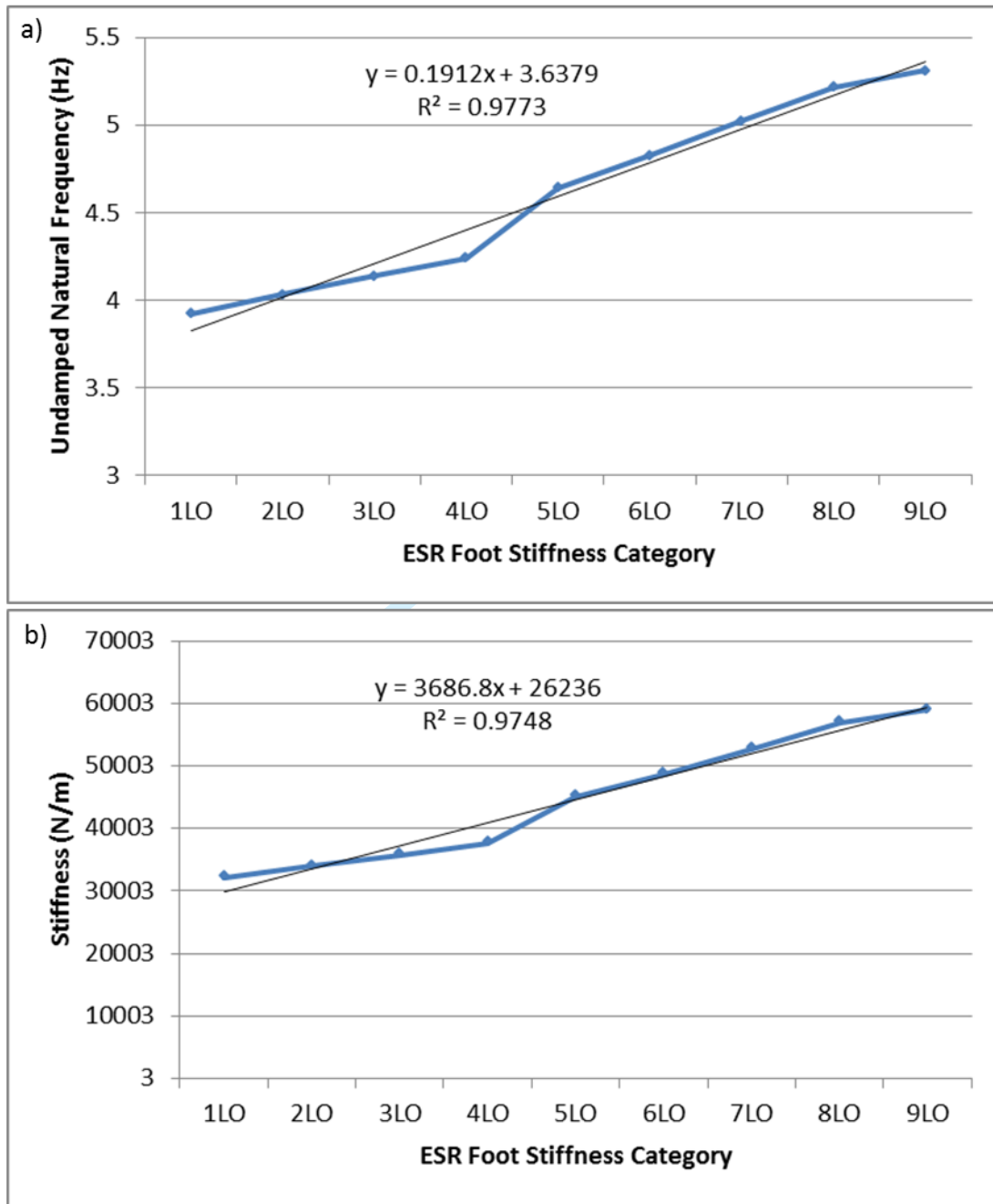


Figure 4: Plot of a) undamped natural frequency (Hz) and b) Stiffness (N/m) against ESR foot stiffness category.

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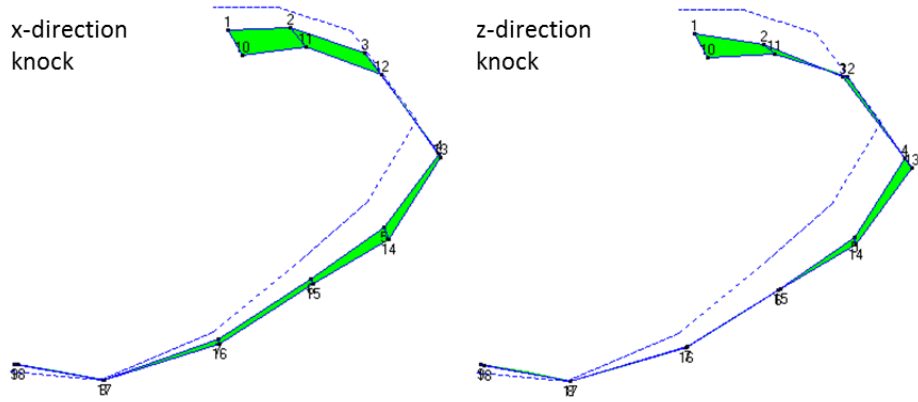


Figure 5: First bending mode of 1LO at 3.94Hz and 3.90Hz with free-free boundary condition knocked in X&Z-direction respectively

Table 1: Flex-Run™ Category Selection Chart

High to Extreme Impact Level	Weight kg	Weight lbs.
1LO	37-44	81-96
2LO	45-52	97-115
3LO	53-59	116-130
4LO	60-68	131-150
5LO	69-77	151-170
6LO	78-88	171-194
7LO	89-100	195-220
8LO	101-116	221-256
9LO	117-130	257-287

Table 2: Detailed instrumentation characteristics

INSTRUMENTS	DESCRIPTION
1LO-9LO Flex-Run feet	Used as test rig to perform modal analysis
PCB Impact Hammer, Model 086C03	Sensitivity: 2.25 mv/N Tip type: medium tip with vinyl cover Hammer mass: 0.16kg Frequency range: 8kHz Amplitude range: ± 2200 N peak
PCB ICP Accelerometer, Model 356B18	Sensitivity: 1000mv/g Frequency range: ($\pm 5\%$) 0.5 to 3000 Hz Amplitude range: ± 5 g peak
NI USB Dynamics Signal Acquisition Module, Model NI-USB 9234	Number of channels: 4 ADC resolution: 24 bits Type of ADC: Delta sigma (with analog pre-filtering)
DASYLab v10	Sampling rate: 2048 samples/sec Block Size: 4096 Channel 1: Impact hammer Channel 2: Accelerometer x-axis Channel 3: Accelerometer y-axis Channel 4: Accelerometer z-axis Averaging: 5 for static conditions Windowing: Force for excitation signal Exponential for response signal
ME'Scope v6.0	To process collected data from NI-DASYLab To define the structural geometry for frequency response function (FRF) modal Analysis To determine the natural frequencies, damping and animated mode shapes after curve fitting process

Table 3: Dynamic characteristics of 1LO-9LO feet with fixed 53kg mass

	1 st Natural Frequency knocked in X-dir.	Damping (%)	1 st Natural Frequency knocked in Z-dir.	Damping (%)
1LO	3.94	1.55	3.90	1.93
2LO	4.02	1.66	4.04	2.06
3LO	4.13	1.65	4.14	1.54
4LO	4.24	1.61	4.24	1.73
5LO	4.64	1.43	4.64	1.63
6LO	4.87	1.65	4.78	1.88
7LO	5.04	1.77	5.00	1.84
8LO	5.21	1.8	5.22	1.81
9LO	5.29	1.54	5.33	1.69

Table 4: Dynamic characteristics of 1LO-9LO based on fixed 53kg mass

Flex-run	Damped natural frequency	Damping (%)	Undamped natural frequency	Stiffness
1LO	3.920	1.740	3.921	32161.72
2LO	4.030	1.860	4.031	33993.51
3LO	4.135	1.595	4.136	35784.68
4LO	4.240	1.670	4.241	37626.04
5LO	4.640	1.530	4.641	45058.14
6LO	4.825	1.765	4.826	48726.54
7LO	5.020	1.805	5.021	52745.4
8LO	5.215	1.805	5.216	56922.73
9LO	5.310	1.615	5.311	59011.67

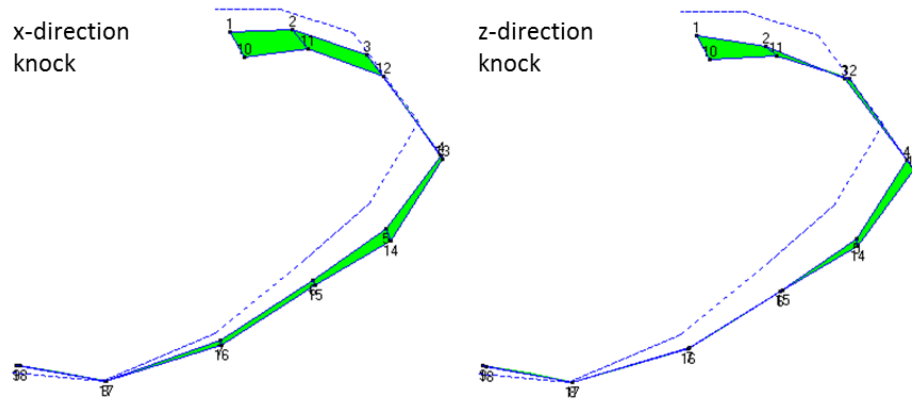


Figure S1: First bending mode of 1LO at 3.94Hz and 3.90Hz with free-free boundary condition knocked in X&Z-direction respectively

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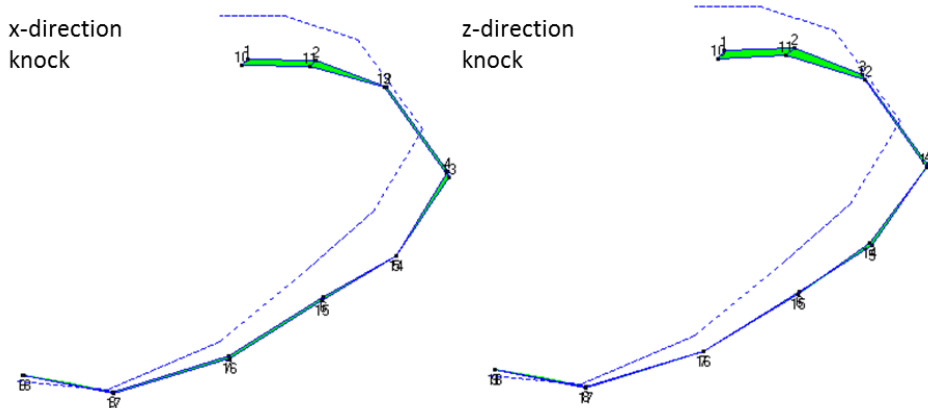


Figure S2: First bending mode of 2LO at 4.02Hz and 4.04Hz with free-free boundary condition knocked in X and Z-direction respectively

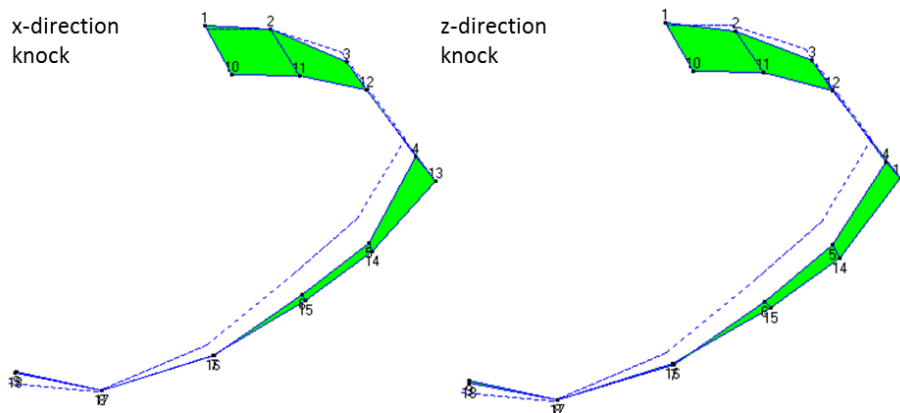


Figure S3: First bending mode of 3LO at 4.13Hz and 4.14Hz with free-free boundary condition knocked in X and Z-direction respectively

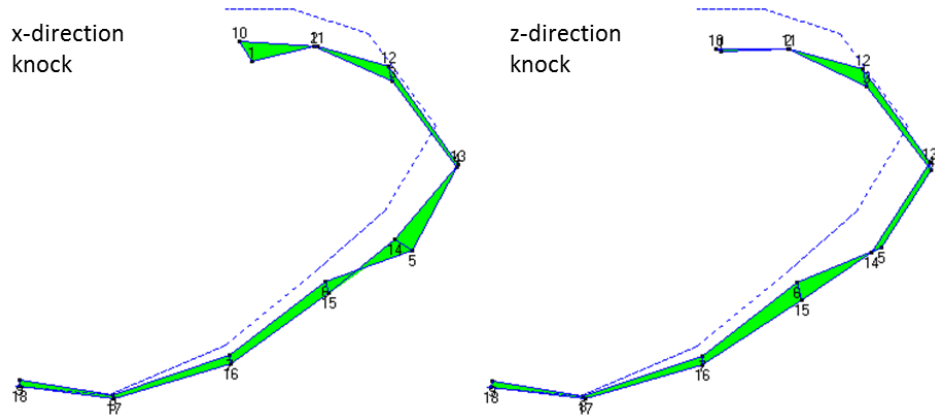


Figure S4: First bending mode of 4LO at 4.24Hz with free-free boundary condition knocked in X and Z-direction respectively

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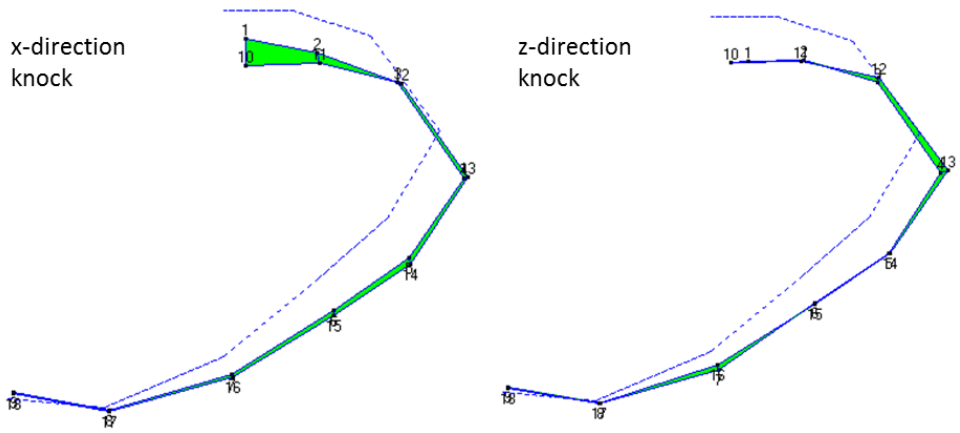


Figure S5: First bending mode of 5LO at 4.64Hz with free-free boundary condition knocked in x and Z-direction respectively

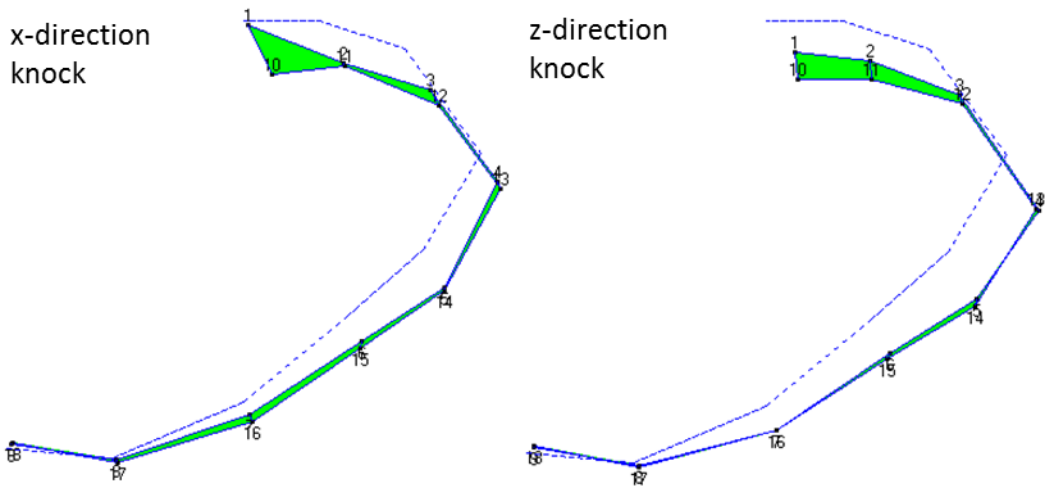


Figure S6: First bending mode of 6LO at 4.87Hz and 4.78Hz with free-free boundary condition knocked in X and Z-direction respectively

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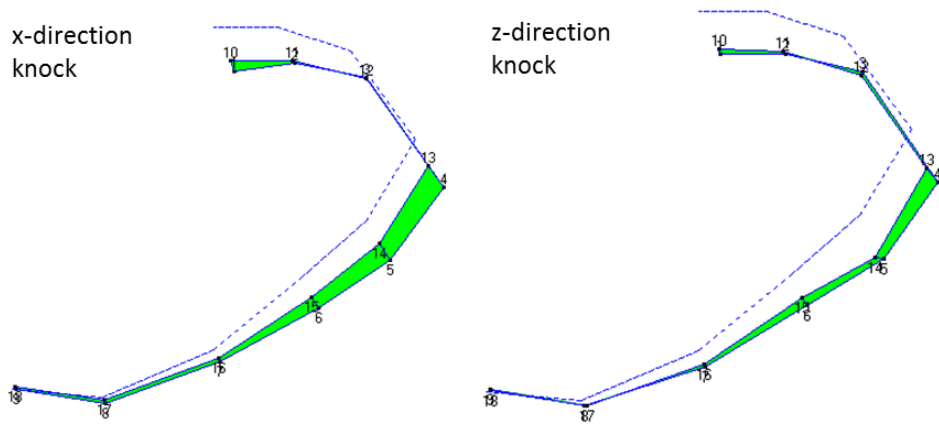


Figure S7: First bending mode of 7LO at 5.04Hz and 5.00Hz with free-free boundary condition knocked in X and Z-direction respectively

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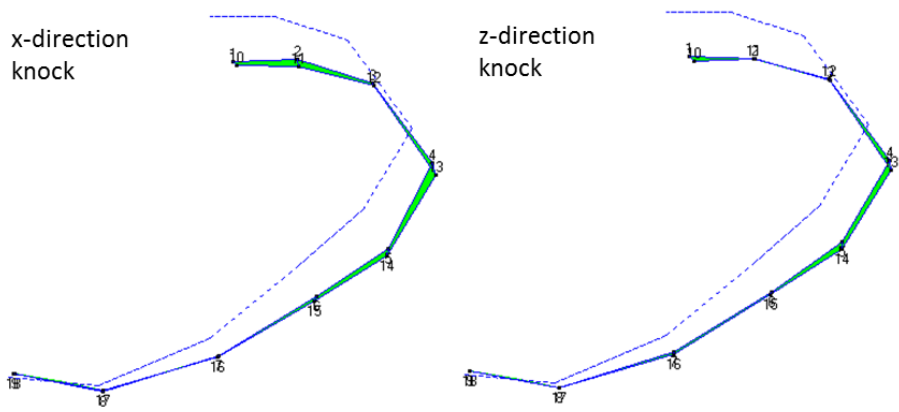


Figure S8: First bending mode of 8LO at 5.21Hz and 5.22Hz with free-free boundary condition knocked in X and Z-direction respectively

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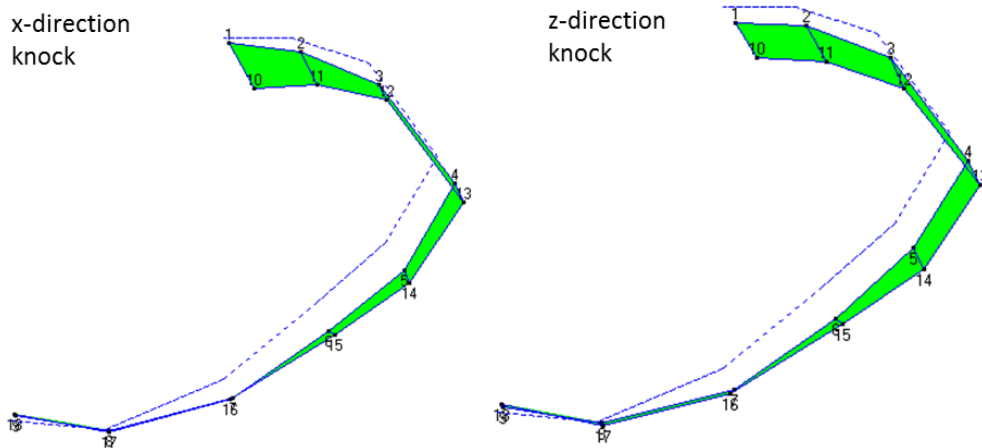


Figure S9: First bending mode of 9LO at 5.29Hz and 5.33Hz with free-free boundary condition knocked in X and Z-direction respectively

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