

# Model Continuity in Discrete Event Simulation: A Framework for Model Driven Development of Simulation Models

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Most of the well known modeling and simulation methodologies state the importance of conceptual modeling in simulation studies and they suggest the use of conceptual models during the simulation model development process. However, only a limited number of methodologies refers to how to move from a conceptual model to an executable simulation model. Besides, existing modeling and simulation methodologies do not typically provide a formal method for model transformations between the models in different stages of the development process. Hence, in the current M&S practice, model continuity is usually not fulfilled. In this article, a model driven development framework for modeling and simulation is presented in order to bridge the gap between different stages of a simulation study and to obtain model continuity. The applicability of the framework is illustrated with a prototype modeling environment and a case study in the discrete event simulation domain.

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## 1. INTRODUCTION

Simulation is the process of developing a model and conducting experiments with it for a specific purpose such as analysis, problem solving, decision support, training, entertainment, testing, research or education [Shannon 1975; Balci 2001]. The fundamental prerequisite for simulation is a model, which is called a *simulation model*. A simulation model is developed through a modeling process, which is called *simulation model development*. The activities in a simulation study are collectively referred to as Modeling and Simulation (M&S) [Balci 2001].

Several methodologies have been proposed to guide modelers through various stages of M&S and to increase the probability of success in simulation studies [Shannon 1975;

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Roberts et al. 1983; Banks 1998; Balci 2012]. Each methodology suggests a body of methods, techniques, procedures, guidelines, patterns and/or tools as well as a number of required steps to develop and execute a simulation model. Almost all of the existing methodologies suggest developing a preliminary conceptual model at the beginning of the simulation model development process. However, only a limited number of methodologies refers to how to move from a conceptual model to an executable simulation model [van der Zee et al. 2010].

In general, conceptual modeling is a process that elicits the general knowledge about a problem or research domain and describes an abstract model that can be refined in subsequent steps to develop a solution for a given problem or a construct for a specific purpose [Olive 2007; Robinson 2008a]. There are several definitions for simulation conceptual modeling. In this research we mainly follow Balci and Robinson [Balci et al. 2011; Balci 2012] and [Robinson 2008a; 2008b; 2011]. Balci et al. [2011] define a simulation conceptual model as a repository of high-level conceptual constructs and knowledge specified in a variety of communicative forms intended to assist in the design of an M&S application. A simulation conceptual model is a non-executable higher level abstraction of the system under study [Fishwick 1995; Kotiadis and Robinson 2008]. It represents a high-level structure and the abstract behavior of a system according to the purpose of the simulation study.

A conceptual model needs to be transformed into a simulation model by using transformation rules, techniques or patterns. However, conceptual models are often not used explicitly in the further stages of the simulation study and a large semantic gap exists between the models at different stages of the simulation project. This gap causes a breach in model continuity in many cases. Model continuity refers to the generation of an approximate morphism relation between the different models within a development process through predefined transformation rules. Model continuity is obtained if the initial and intermediate models are effectively consumed in the later steps of a development process and the modeling relation is preserved [Hu and Zeigler 2005]. The main advantages of supporting model continuity are increasing the productivity, maintainability, consistency and quality of a simulation study.

In order to address the model continuity problem, our research suggests the application of a Model Driven Development (MDD) approach throughout the whole set of M&S activities and proposes a formal MDD framework for modeling and simulation. MDD is a software engineering methodology that prescribes the systematic use of models as the primary means of a development process [Kleppe et al. 2003]. MDD introduces model transformations between the models at different abstraction levels and proposes the use of metamodels for specifying modeling languages. In MDD, models are transformed into other models in order to (semi)automatically generate the final software system. Due to the similarities between software development and simulation model development, MDD could potentially be a cost and effort saving approach for the M&S community, while taking into account the peculiarities of simulation such as data intensiveness and time dependence.

MDD approaches were introduced to M&S in 2001 when Bakshi et al. [2001] presented a practical application of Model Integrated Computing (MIC) into embedded system design and simulation. They provided a formal paradigm for specification of structural and behavioral aspects of embedded systems, an integrated model-based approach, and a unified software environment for embedded system design and simulation. One year later, Vangheluwe et al. [2002] introduced metamodeling and model transformation concepts for modeling and simulation. They present an approach to integrate three orthogonal directions of M&S research: multi-formalism modeling, model abstraction, and metamodeling.

In the context of MDD, metamodeling is the process of complete and precise specification of a modeling language in the form of a metamodel. For many years, the term 'metamodeling' was used in the simulation field in a different context. Here, metamodeling referred to constructing computationally faster models with the same input-output behavior as complex simulation models [Barton 1998; Kleijnen 2009]. Such a metamodel is now called a 'surrogate model'. Surrogate models mimic the complex behavior of an underlying simulation model. Metamodeling in the context of MDD has been introduced to simulation later.

Tolk and Muguira [2004] introduced the Model Driven Architecture (MDA) [OMG 2003] for distributed simulation. They presented methods to merge the High Level Architecture (HLA) and the Discrete Event System Specification (DEVS) within the MDA framework. After the introduction of these initial ideas, there have been many efforts to use MDD concepts in M&S. In some cases, metamodeling was used to describe domain specific modeling languages for one stage in the M&S methodology [Duarte and de Lara 2009; Levytskyy et al. 2003; Lei et al. 2009; Touraille et al. 2011; Sarjoughian and Markid 2012]. In all of these applications, MDD tools were mainly used for automatic code generation from a system specification and they ignored the more abstract conceptual models.

More unified solutions are presented by following either the MDA approach [DeAntoni and Babau 2005; Guiffard et al. 2006; D'Ambrogio et al. 2010; Garro et al. 2013; Sarjoughian and Markid 2012] or the MIC approach [Topçu et al. 2008; Çetinkaya et al. 2010; Ledeczi et al. 2003]. Guiffard et al. [2006] provide a study that aims at applying a model driven approach to M&S in the military domain. Their prototype demonstrates that the automated transformation from a source model to executable source code is possible. D'Ambrogio et al. [2010] introduce a model driven approach for the development of DEVS simulation models. Their approach allows to specify DEVS models in UML, and it automates the generation of DEVS simulations that make use of the DEVS Service Oriented Architecture implementation that is presented by Mittal et al. [2009]. Garro et al. [2013] propose an MDA-based process for agent-based modeling and simulation (MDA4ABMS) that uses the agent modeling framework of the Eclipse Agent Modeling Platform project. The MDA4ABMS process allows the automatic production of platform specific simulation models starting from platform independent simulation models. The source code can be automatically generated, which results in a significant reduction of programming and implementation efforts. Topçu et al. [2008] propose the Federation Architecture Metamodel (FAMM) for describing the architecture of a HLA compliant federation. FAMM supports the behavioral description of federates based on sequence charts and it formalizes the standard HLA object model and federate interface specification.

In addition to the MDA and MIC approaches, UML or SysML (Systems Modeling Language) based methods for metamodel-based simulation have been proposed by either using extension mechanisms, or model transformations [Pop et al. 2007; Schamai et al. 2009; Kerzhner et al. 2011; Batarseh and McGinnis 2012; Reichwein et al. 2012]. Pop et al. [2007] propose a UML profile for Modelica called ModelicaML (Modelica Modeling Language) which is a graphical modeling language that enables users to depict a Modelica simulation model graphically. The Modelica language provides a sound way for defining models in a declarative, modular, and hierarchical way [Fritzson 2010]. ModelicaML extends the graphical modeling capabilities of Modelica by using UML diagrams. ModelicaML enables the generation of executable Modelica code. Schamai et al. [2009] extended ModelicaML with constructs for model behavior. They also discuss the usage of executable UML state machines for system modeling and present a proof of concept for the translation of UML state machines into executable Modelica code [Schamai et al. 2010; Schamai et al. 2013].

Paredis and Johnson [2008] present a generic approach for defining automated, bidirectional transformations between SysML and domain specific languages. They propose metamodels for a specific domain and a SysML profile in which the domain specific constructs are mapped to stereotypes. Then, graph transformations are created that use the domain specific metamodel and the corresponding SysML profile. This approach has been formalized in [Paredis et al. 2010] for the mapping of SysML to Modelica. The SysML-Modelica transformation is specified between the profile constructs and the Modelica language constructs as captured in the Modelica metamodel. The transformation approach simplifies the transformation to Modelica, and facilitates model reuse by using existing model libraries.

In addition to these approaches, Risco-Martín et al. [2009] present a UML-based DEVS simulation method that is part of the DEVS Unified Process (DUNIP). DUNIP proposes a process that uses the DEVS formalism as a basis for automated generation of models from various requirement specifications [Mittal et al. 2007; Mittal et al. 2008]. Mittal and Douglass [2012] show that an underlying DEVS metamodel provides model reusability across different platforms. Furthermore, there have been studies to use ontologies during the development of simulation models to provide a substantive basis for defining a system structure for a domain [Silver et al. 2007; McGinnis et al. 2011; Tolk and Miller 2011].

Although the aforementioned efforts show the applicability of the MDD approach in the simulation field, most of the applications are formalism or specification dependent. As a result, to the best of our knowledge, there is no generic theoretical framework that provides guidance for formal model transformations while moving from a conceptual model to an executable simulation model. One of the reasons for this issue could be that there is not a commonly accepted terminology and formal specification for MDD [Favre 2004]. Although MDD has been advocated as a cost and effort saving development approach for software projects [Selic 2003], the MDD principles for the M&S field are currently only described informally. The M&S research community has recently started to move toward a theoretical framework for simulation such as the work of Tolk et al. [2013] and Diallo et al. [2011], which use model theory.

The contribution of this paper is to bridge the gap between different stages of a simulation study in a formal manner as well as proposing a theory for MDD within M&S. A model driven development framework for modeling and simulation, called MDD4MS, has already been introduced in [Çetinkaya et al. 2011]. The proposed framework defines three metamodels for different stages of a simulation study and suggests model transformations based on these metamodels. The improved version of the framework is represented in [Çetinkaya et al. 2013]. The MDD4MS prototype implementation is illustrated in [Çetinkaya et al. 2012; 2013]. Although our earlier work introduced the initial ideas, basic concepts and practical aspects, the formal theory of our framework is presented in this article. In this theory, MDD principles have been clearly defined and specified for the M&S field. A comprehensive definition of the MDD4MS framework is presented and formal relations between the key concepts are defined.

The next section provides a comparative analysis between the selected M&S methodologies in order to highlight the common steps in simulation studies. Section 3 proposes the theory of modeling, metamodeling, model transformation and MDD. Section 4 introduces a mapping between the MDD concepts and the M&S concepts. Section 5 proposes the theory of the MDD4MS framework. Section 6 presents a case study with the MDD4MS prototype to illustrate the applicability of the framework in the discrete event simulation domain. Finally, conclusions are drawn in Section 7.

## 2. SIMULATION MODEL DEVELOPMENT AS A MODEL-BASED PROCESS

In this section, a set of M&S methodologies will be analyzed in order to see if they can be identified as a model-based approach and if an MDD approach can be incorporated into these methodologies. Each methodology prescribes a number of steps for conducting a simulation study [Balci 2012]. Looking at the existing methodologies, some similar terms and patterns can be distinguished. Each simulation study roughly consist of four main stages; problem definition, model development, simulation model execution and analysis of results. In the problem definition stage, the purpose of the simulation study, the boundaries of the problem and the requirements are defined. In the simulation model development stage, an executable simulation model is developed, which is ready to be executed on a platform, and data for the simulation study is collected. Developing a conceptual model is often recommended at the beginning of this stage. In the simulation model execution stage, experiments are designed and the simulation model is executed using a subset of the collected data. In the analysis stage, the experimentation results are presented and analyzed.

Table I presents an analysis of different M&S methodologies. Each methodology is evaluated according to a set of questions to analyze their support for model continuity [Atkinson and Kühne 2003]. The results in Table I show that all of the methodologies introduce multiple steps for carrying out a simulation study. Regarding the outputs of these steps it is identified that the development process highly relies on models such as conceptual models, formal models, computer models, and experimentation models.

All of the methodologies require a conceptualization step and many of them suggest to transform the conceptual model into a simulation model, but do not formally define how to do that. All of the methodologies prepare for computer simulation and require a programming step or model coding step. Some of them mention automatic code generation. Therefore, M&S can be identified as a model-based process [Ören 2007] and an MDD method can be incorporated into these methodologies. On the other hand, some of the methodologies are lacking a formal specification step which is important to separate the formal system specification from programming concerns. Moreover, almost all of the methodologies ignore model transformations and none of them provides formal model transformation methods between the models in different step. Hence, model continuity is not supported. Well-defined model driven approaches are needed to provide model continuity. The MDD4MS framework provides a generic MDD framework for M&S that supports model continuity [Çetinkaya et al. 2011]. It provides a formalism independent solution via formalizing the steps which can be incorporated into existing methodologies. Before presenting the theory of the MDD4MS framework, the next section gives a formal definition of models, modeling languages, metamodels, and model transformations, and it proposes a theory for MDD within M&S.

## 3. THEORY OF MODELING, METAMODELING AND MODEL DRIVEN DEVELOPMENT

This section provides a theoretical basis for modeling, metamodeling and model transformations. Although a sound and comprehensive reference is lacking in software engineering literature, the related work on mathematical explanation of MDD concepts [Favre 2004; Kühne 2006; Jouault and Bézivin 2006; Jackson and Sztipanovits 2009] provided us the preliminary definitions and ideas.

### 3.1. What is a Model?

Modeling is the process of representing a source system for a specific purpose in a form that is ultimately useful for an interpreter. The concrete form that represents the system is called the model. Broadly speaking, a model is a representation of something. The represented thing is called the source that can for instance be an object,

Table I. Analysis of M&amp;S methodologies according to their support for model continuity.

<b>Analysis criteria</b>	[Shannon 1975] p.24	[Roberts et al. 1983] p.8	[Nance 1984] p.76	[Fishwick 1995] p.4	[Shannon 1998] p.9	[Banks 1998] p.15	[Law 2003] p.67	[Robinson 2004] p.52	[Wainer 2009] p.27	[van Daalen et al. 2009] p.1129	[Sargent 2010] p.169	[Balci 2012] p.4
Has multiple models?	Y	Y	Y	Y	Y	Y	Y	Y	Y	Y	Y	Y
How many models?	2	3	4	6	2	2	2	2	3	3	2	2
Has a conceptualization step?	P <sup>1</sup>	P <sup>1</sup>	Y	Y	P <sup>1</sup>	Y	Y	Y	Y	Y	Y	Y
Has a formal specification step?	N	Y	N	Y	N	N	N	P <sup>3</sup>	Y	Y	P <sup>3</sup>	P <sup>3</sup>
Has a programming step?	Y	Y	Y	Y	Y	Y	Y	Y	Y	Y	Y	Y
Proposes conceptual model transformation?	N	P	Y	Y	P	Y	N	Y	N	Y	N	Y
Proposes automatic code generation?	N	N	Y	Y	N	Y	N	N	N	N	N	Y
Provides formal model transformations?	N	N	N	P <sup>2</sup>	N	N	N	N	N	N	N	N

Note: Y: Yes, N: No, P: Partially.

<sup>1</sup>Conceptual model is not mentioned, but a diagram such as a flow diagram is suggested.

<sup>2</sup>The framework does not provide formal transformation methods, but proposes some heuristics, explicit translation rules and general code writing rules.

<sup>3</sup>A software specific description that determines how to structure the model is proposed.

an idea, a phenomenon, an organization, a process, or an event. A model can also be a representation of another model. In systems thinking, a model is a representation of a source system. We see a system as a set of interrelated elements [Klir 1969; von Bertalanffy 1968]. A model is developed for a purpose related to the source system [Klir 1969; Shannon 1975; Ackoff 1978]. This purpose can be achieved by executing or interpreting the model and thereby gaining knowledge about the source system. The interpretation can only be validated in a given context. The context includes the purpose of the modeling process, information about the environment of the source system, and the constraints, assumptions and facts that affect the modeling process. A context can be formally defined in a model as well [Theodorakis et al. 2002].

A model is specified in a modeling language [Milicev 2009]. A modeling language consists of an abstract syntax, concrete syntax and semantics [Atkinson and Kühne 2003]. The abstract syntax describes the vocabulary of the concepts provided by the modeling language and how they can be connected to create models. The abstract syntax consists of the concepts, the relationships and well-formedness rules, where well-formedness rules state how the concepts may be combined. The concrete syntax provides a way to show the modeling elements in a concrete form which we see and work with on paper or on the computer screen [Rumpe 1998]. The expression generated with the concrete syntax is called the model and it is often in a structured textual form. The semantics of a modeling language is the additional information to explain what the abstract syntax actually means. We use the grammar notion of formal language theory to define the abstract syntax and we assume that a default concrete syntax is provided by the

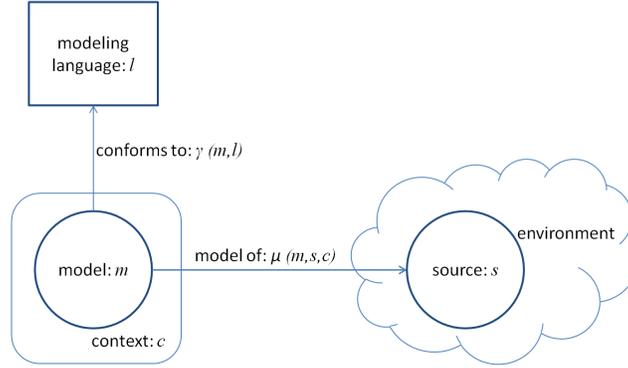


Fig. 1. The relationships between model, source and language.

metalanguage [see Appendix A]. In this paper, we use the following primitive terms and relations:

$S$  is the infinite set of all source systems. Variables such as “ $s, s_1, s_2, \dots$ ” range over  $S$ .

$C$  is the infinite set of all contexts. Variables such as “ $c, c_1, c_2, \dots$ ” range over  $C$ .

$L$  is the infinite set of all formal languages. Variables such as “ $l, l_1, l_2, \dots$ ” range over  $L$ .

The usual set operations are applicable to  $S$ ,  $C$  and  $L$  such as union, intersection, difference, complement, subset, proper subset, cartesian product and powerset. The  $+$  function  $c_1 + c_2 : C \times C \rightarrow C$  is used to represent the composition of two contexts, where  $c_1 + c_1 = c_1$ ,  $c_1 + c_2 = c_2 + c_1$  and  $c_1 \leq c_1 + c_2$ . We next propose the following definitions using formal language theory.

**Definition 3.1 (Model).** Let  $g = \{T, N, I, P\}$  be a grammar where  $T, N, I$  and  $P$  are defined in Appendix A, and the language that  $g$  generates is  $l(g)$ . If an expression  $m \in l(g)$  is a representation of a source system  $s$  within a context  $c$ , then  $m$  is said to be a model of  $s$  in  $c$ . The infinite set of all models is denoted with  $M$ . Variables such as “ $m, m_1, m_2, \dots$ ” range over  $M$ . The ternary relation ‘model-of’ is denoted with  $\mu: M \times S \times C$ .

**Definition 3.2 (Conforms-to relation).** If an expression  $m \in l(g)$  and  $m \in M$ , then the language  $l$  is a modeling language and  $m$  conforms-to  $l$ . The binary relation ‘conforms-to’ is denoted with  $\gamma: M \times L$ .

**Axiom 3.3 (Transitive- $\mu$ ).**  $\mu(x, y, c_1) \wedge \mu(y, z, c_2) \wedge y \in M \Rightarrow \mu(x, z, c_1 + c_2)$ .

Figure 1 shows the relationships between a model, a source and a language. Although the terminal symbols of the grammar provide a default concrete syntax (primary view), it is possible to define other concrete syntax mappings (secondary views). For example, it is very common that a model has a textual view and a diagrammatic view in computer science. We suggest using an extended grammar to define a mapping from the default concrete syntax to a set of concrete symbols. In this way, all of the possible final or intermediate productions of a given grammar with both terminal and non-terminal symbols can be included in the mapping. The language defined with the extended grammar allows defining composed modeling elements for a modeling language. Most important is that the primary view has all the specified information and the secondary views will be syntactically either equivalent to or weaker than the primary view.

*Definition 3.4 (Extended grammar).* Let  $g = \{T, N, I, P\}$  be a grammar, and  $l(g)$  be a modeling language. Let  $\hat{g} = \{T \cup N, N, I, P\}$  be another grammar, and  $\hat{l}(\hat{g})$  be all expressions generated by  $\hat{g}$ .  $\hat{l}$  includes all of the possible expressions with both terminal and non-terminal symbols of  $g$ . Hence,  $l \subseteq \hat{l}$ . The grammar  $\hat{g}$  is the extended grammar of  $g$ .

*Definition 3.5 (Concrete syntax mapping).* Let  $g = \{T, N, I, P\}$  be a grammar, and  $l(g)$  be a modeling language. A concrete syntax mapping for  $l(g)$  is a binary relation from  $\hat{l}(\hat{g})$  to  $cs$ , where  $cs$  is a set of concrete symbols, and the relation is denoted as  $\psi(\hat{l}(\hat{g}), cs)$ .

*Definition 3.6 (Secondary view).* Let  $m \in M$  be a model that conforms to a modeling language  $l(g)$ . For a given set of concrete symbols  $cs$ , if  $m$  can be mapped to an expression  $v \in cs^*$ , by using a concrete syntax mapping  $\psi(\hat{l}(\hat{g}), cs)$ , then  $v$  is a secondary view of the model  $m$ .  $cs^*$  is the infinite set of all expressions, which can be obtained by composing zero or more symbols from  $cs$ . The infinite set of all secondary views is denoted with  $V$ . Variables such as “ $v, v_1, v_2, \dots$ ” range over  $V$ .

In order to specify, view or change models on computer platforms, we use model editors. A model editor for a modeling language  $l$  provides a way to specify models according to the syntax of  $l$  and save them according to a specific file format. In addition, the editor uses a language parser to decompose a model according to the abstract syntax of  $l$  [Muller et al. 2008] and shows the model on the screen using one or more views from  $V$ . If a concrete syntax mapping is defined, the editor can show a different view of the model, e.g., by changing the shape of a specific type of element in a model. Although secondary views of a model are based on the default concrete syntax, semantically they can be more powerful than the primary view. In many cases, the model editor provides extra features such as verification or syntax highlighting. Most model editors are also capable of hiding aspects of a model for the user. In this case, the concrete syntax remains unchanged. It is not easy to define a grammar and a concrete syntax for a modeling language from scratch. Furthermore, developing a model editor for a language requires advanced software engineering skills. The metamodeling approach, introduced in the next section, solves most of these problems.

### 3.2. Metamodeling

Metamodeling is the process of specifying a grammar of a modeling language in the form of a model, which in turn can be used to specify models in that language. Hence, metamodeling is a modeling process where the source is a grammar. The following definitions can be derived from the earlier ones.

*Definition 3.7 (Metamodel).* Let  $mm \in M$  is a model and  $\exists \mu(mm, s, c)$ , where  $s \in S$  and  $c \in C$ . A model  $mm$  is a metamodel if, and only if,  $s$  is a grammar. The infinite set of all metamodels is denoted with  $M'$ , where  $M' \subset M$ . Variables such as “ $mm, mm_1, mm_2, \dots$ ” range over  $M'$ .

*Definition 3.8 (Metamodeling language).* For any  $mm \in M'$  and  $\gamma(mm, l)$ , the language  $l$  is a metamodeling language. The infinite set of all metamodeling languages is denoted with  $L'$ , where  $L' \subset L$ . Variables such as “ $l, l'_1, l'_2, \dots$ ” range over  $L'$ .

Similar to a modeling language, a metamodeling language has one abstract syntax and at least one concrete syntax. In order to specify, view or change metamodels on computer platforms, we use metamodel editors. All information about models can also be applied to metamodels and metamodeling languages.

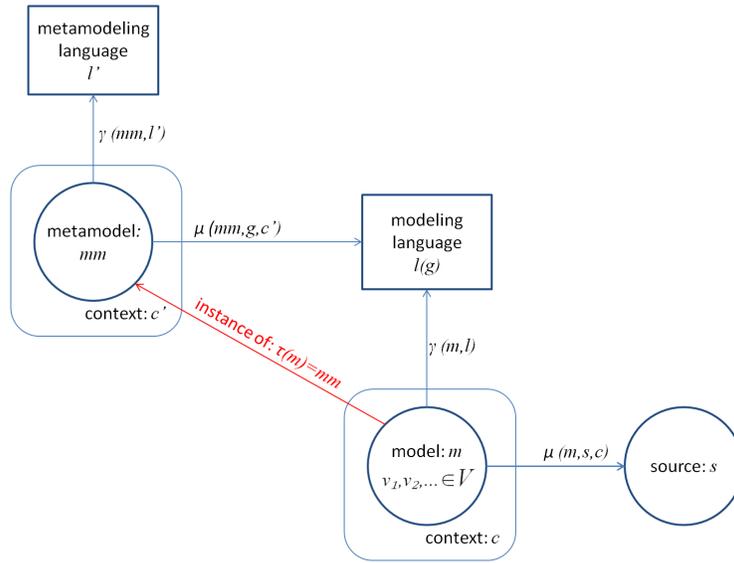


Fig. 2. Metamodeling.

The purpose of the metamodeling process is representing the grammar of a modeling language in order to provide a proper way to develop models with that language. For example, instead of developing a model for a specific problem in a certain domain, first a metamodel which defines the concepts that apply to a larger set of problems in that domain is specified. Then, the metamodel is used to develop a specific model. In this case, a model is said to be an instance-of the metamodel. If a model  $m$  is an instance-of a metamodel  $mm$ , where  $mm$  is a model of a grammar  $g$ , then the model  $m$  conforms-to  $l(g)$ . Figure 2 illustrates the relations between a model and a metamodel. If  $mm$  is a model of a grammar  $g$  then we write  $l(mm) \cong l(g)$ .

**Definition 3.9 (Instance-of relation).** Let  $m \in M'$  be a metamodel,  $m \in M$  be a model, and  $\gamma(m, l(mm))$ . Then,  $m$  is an instance-of  $mm$  if, and only if, every element of  $m$  is an instance-of some element in  $mm$ . The binary function ‘is-instance-of’ is denoted with  $\tau(m) : M \rightarrow M'$ .

**Lemma 3.10 (Formalized conforms-to).**  $(\tau(x) = y) \Rightarrow \gamma(x, l(y))$  (by definition 3.9).

Popular metamodeling languages are: MOF [OMG 2006], Ecore [Eclipse 2014], KM3 [IRISA 2011] and MetaGME [Emerson et al. 2004]. One can easily notice that the metamodeling pattern can be applied again, and a metamodeling language can also be defined with a metamodel. In this case, the metamodel which is a model of the grammar of a metamodeling language is called a meta-metamodel and it is specified in a meta-metamodeling language.

Although, it is possible to increase the number of metamodeling levels theoretically, a 4-level metamodeling architecture that was introduced in the UML specification by OMG in 1999 [OMG 1999] is generally used in practice. In the metamodeling architecture introduced by OMG, the M3-level is for representing a metamodeling language as a meta-metamodel; the M2-level is for representing a modeling language as a metamodel; the M1-level is for representing a system without specific user data; and the M0-level is for representing a system with user data. In addition, OMG introduces the concept of a UML profile at the M1-level. It is a way of specifying an incomplete (pa-

parameterizable) model, so that the details can be filled in later. We will use the term *template models* for these incomplete models within the modeling process. A set of template models in a modeling language for a domain is called a domain specific modeling library, whereas the set of modeling elements provided by the grammar of the language is called the basic (or core) modeling library [Atkinson and Kühne 2002]. We accept these features as implementation specific concepts, and many state-of-the-art metamodel editors provide them.

In general, the metamodel editors provide extra features such as model-to-model transformation, code generation or model interpretation. In this case, the complete tool set is called a metamodeling environment. A full featured metamodeling environment provides a way to specify a metamodel  $mm$  and automatically generate a model editor for the modeling language  $l(mm)$ . The resulting editor may either work within the metamodeling environment, or less commonly be produced as a separate standalone program. Once we have metamodels and models, we can discuss metamodel-based model transformations. The next section explains model transformations in the MDD context.

### 3.3. Model Transformations

A model transformation is the process of converting a model into another form according to a set of transformation rules. According to the output type or target language of the process, the model transformation can be classified as a model to model (M2M) transformation, a model to text (M2T) transformation, or a model to code transformation (M2C or code generation). As the name implies, a M2M transformation converts a model into another model, whereas M2T transformation converts a model into text. M2T transformation is generally used for supportive document creation. If the model is used to generate source code, then the transformation is called code generation. Well known M2M transformation languages are ATL (ATLAS Transformation Language) and QVT (Query/View/Transformation) [Çetinkaya and Verbraeck 2011].

In the MDD context, we are only interested in formal model transformations. A formal transformation requires that the models are specified in well-defined modeling languages and the rules are defined with a model transformation language. A transformation rule consists of two parts: a left-hand side that accesses the given model; and a right-hand side that generates the target system. Hence, a model transformation is performed with a well-defined model transformation pattern. In order to provide model continuity, the target model should contain as much as possible from the source model and the initial modeling relation should be preserved [Ehrig and Ermel 2008].

*Definition 3.11 (Model transformation pattern).* A model transformation pattern  $p$  is defined as a triple  $p = \{l_x, l_y, r\}$ , where  
 $l_x$  is the source modeling language,  
 $l_y$  is the target language (any language such as a programming language, a modeling language or any well-defined language),  
 $r$  is a finite set of transformation rules from  $l_x$  to  $l_y$  which are defined with a model transformation language.

The infinite set of all model transformation patterns is denoted with  $P$ . Variables such as “ $p, p_1, p_2, \dots$ ” range over  $P$ .

*Definition 3.12 (Formal model transformation).* Let  $m \in M$  be a model that conforms to  $l_1$ , and  $p = \{l_1, l_2, r\}$  be a model transformation pattern. If an expression  $e \in l_2$  is derived from  $m$  by applying  $p$ , then the derivation is called a formal model transformation. We say that  $m$  is transformed-to  $e$  by applying  $p$  and denote it as  $\theta(m, p) = e$ .

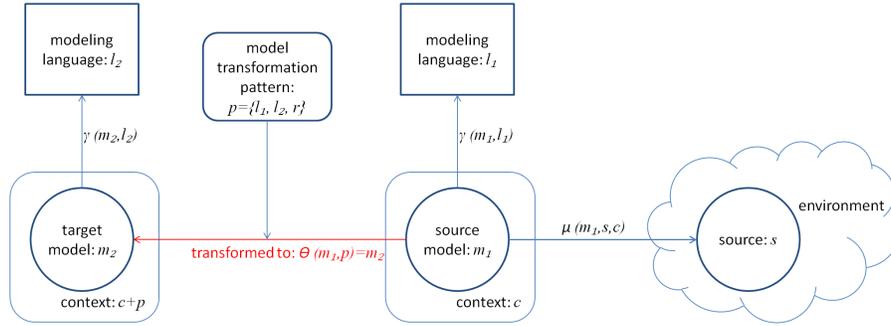


Fig. 3. The relationships in a model-to-model transformation.

**Definition 3.13 (Formal model-to-model transformation).** If  $\theta(x, p) = y$  and  $y \in M$ , then the transformation is called a formal model-to-model transformation.

**Theorem 3.14.** If the model transformation pattern  $p$  preserves the system related information in the source model, then

$$(\theta(x, p) = y) \wedge \mu(x, s, c) \wedge (y \in M) \Rightarrow \mu(y, s, c + p).$$

Figure 3 shows the relationships in a model-to-model transformation.

**Definition 3.15 (Code generation).** If  $\theta(x, p) = y$  and  $y$  is a source code in a software programming language, then the transformation is called code generation.

**Lemma 3.16.**  $(\theta(x, p) = y) \wedge (p = \{l_1, l_2, r\}) \Rightarrow \gamma(x, l_1)$  (by definition 3.12).

**Lemma 3.17.**  $(\theta(x, p) = y) \wedge (y \in M) \wedge (p = \{l_1, l_2, r\}) \Rightarrow \gamma(y, l_2)$  (by definition 3.12 and definition 3.13).

For a metamodel-based model transformation, either the source model is an instance of a metamodel or the target model is an instance of a metamodel, or preferably both.

**Lemma 3.18.**  $(\theta(x, p) = y) \wedge (p = \{l(mm_1), l_2, r\}) \wedge (mm_1 \in M') \Rightarrow (\tau(x) = mm_1)$  (by definition 3.12).

**Lemma 3.19.**  $(\theta(x, p) = y) \wedge (y \in M) \wedge (p = \{l_1, l(mm_2), r\}) \wedge (mm_2 \in M') \Rightarrow (\tau(y) = mm_2)$  (by definition 3.12 and definition 3.13).

The goal of model transformations is to automatically generate different representations of a system at different abstraction levels and to enable the reuse of information that was once modeled. A key point here is the model transformation language. A model transformation language is a language that provides a way to write transformation rules for the expressions of a formal grammar. Given two formal grammars (one is for the source language and one is for the target language) and a model specified in the source language, a language parser can parse the transformation rules; an interpreter can interpret the source model; and a model transformation engine can apply a consecutive set of the rules on the source model and generate a target model according to the interpretation. A model transformation tool combines all of these concepts and it is usually embedded in a metamodeling environment. Sometimes, a model transformation is called a graph transformation if the models are specified as graphs, and the transformation tool is then called a graph transformation tool [Agrawal et al. 2004]. A model transformation is also known as a model morphism [Agostinho et al. 2010].

The presented definitions and relations provide a generic framework allowing anything to be the source of a modeling process, i.e. anything can be modeled. For exam-

ple, it is possible to develop a model of a model transformation pattern [Bézivin et al. 2006]. In addition, a metamodel can be defined to represent the grammar of the model transformation language.

In the M&S domain, metamodeling has been applied for formal transformations. For example, Paredis and Johnson [2008] discuss the use of a graph transformation approach to define a mapping between domain specific metamodels and a corresponding SysML profile. Paredis et al. [2010] provide an overview of the formal transformation between SysML and Modelica. Risco-Martín et al. [2009] propose XML/XSLT-based transformations to generate executable DEVS models from UML models by using a DEVS metamodel. McGinnis et al. [2011] discuss how ontologies can be effectively deployed in simulation and they present formal transformations to generate Arena and AnyLogic models from SysML models. All of these studies show that the transfer of modeling information between different models is improved by formalizing the steps.

### 3.4. What is an MDD process?

Model driven development is a software engineering methodology that uses well-defined modeling languages to specify models, and applies model transformations to automatically generate source code from an initial software design model. In an MDD approach, there is usually a chain of several M2M transformations and a final model-to-code transformation. By using the definitions given in the previous sections, we define an MDD process as:

*Definition 3.20 (MDD process).* A model driven development process for a software application development is defined as a tuple

$$mdd = \{n, MML, ML, MO, SL, pl, MTP, STP, MT, sc, TO\}$$

where

$n$  is the number of models,

$MML = \{l'_0, l'_1, \dots, l'_{n-1}\}$  is an ordered set of metamodeling languages (can be defined with meta-metamodels),

$ML = \{l_0(mm_0), l_1(mm_1), \dots, l_{n-1}(mm_{n-1}) \mid \gamma(mm_i, l'_i)(0 \leq i < n)\}$  is an ordered set of modeling languages (preferably defined with metamodels),

$MO = \{m_0, m_1, \dots, m_{n-1} \mid \gamma(m_i, l_i)(0 \leq i < n)\}$  is an ordered set of models,  $m_0$  is the initial model and  $m_{n-1}$  is the final model,

$SL$  is a set of supplementary languages (including at least a model transformation language for writing transformation rules),

$pl$  is a programming language for final code generation,

$MTP = \{p_0, p_1, \dots, p_{n-2}, p_{n-1}\}$  is a set of formal model transformation patterns, where  $p_i$  is a model-to-model transformation pattern,  $p_{n-1}$  is a code generation pattern, and  $(p_{n-1} = \{l_{n-1}(mm_{n-1}), pl, r\}) \in MTP$  (including at least the final code generation pattern),

$STP$  is a set of other supplementary model transformation patterns,

$MT = \{(\theta(x, p) = y) \mid (x \in M) \wedge (p \in MTP)\}$  is a set of formal model transformations, where  $(\theta(m_{n-1}, p_{n-1}) = sc) \in MT$  (including at least the final code generation),

$sc$  is the final source code,

$TO$  is a set of tools to ease the activities.

The most notable advantages of MDD are rapid software development and increased productivity. Hence, computerized tool support is very important in MDD approaches. We recommend the following basic tools for MDD: a full-featured metamodeling environment, a set of model editors and a set of model transformation tools [Atkinson and Kühne 2003; Emerson et al. 2004].

Although MDD principles are described by different specifications, the most commonly used terminology is introduced by MDA [OMG 2003]. MDA introduces three types of viewpoints: The computation independent viewpoint focuses on the environment of the system and the requirements for the system. The platform independent viewpoint focuses on the structure and operation of the system while hiding the details necessary for a particular platform. The platform specific viewpoint focuses on the use of a specific platform by a system. Based on these viewpoints, three types of models are used in MDA: A Computation Independent Model (CIM) is a representation of a system from the computation independent viewpoint that does not show the details of the system. A Platform Independent Model (PIM) is a representation of a system that exhibits a specified degree of platform independence to be usable with a number of different platforms. A Platform Specific Model (PSM) is a representation of a system that combines the specifications in the PIM with the details that specify how that system uses a particular type of platform. MDA also defines the PIM-to-PSM transformation and requires that the PSM will include the source code. However, a CIM-to-PIM transformation is not clearly defined in MDA since a CIM is assumed to be a kind of requirements specification.

When following the MDA viewpoints, we can say that at least three types of models are produced during a software development lifecycle: a CIM for the analysis stage, a PIM for the design stage, and a PSM for the implementation stage [Sommerville 2007]. The final source code will be generated from the PSM. In more generic terms, an MDD process is supposed to have an initial model, a number of intermediate models, a final model and final source code. The aim is to obtain a large part of the models and the final code through successive model transformations. An MDD process supports model continuity by formal model transformations.

*Definition 3.21 (Model continuity).* Let  $mdd$  be an MDD process,  $m_0$  be the initial model of this process and  $\mu(m_0, s, c)$ .

We say that model continuity is obtained in an  $mdd$  process if, and only if  $n \geq 2$  and  $\mu(m_{final}, s, c + x)$ , where  $m_{final}$  is the final model of the MDD process, it is generated through formal model transformations, and it preserves the modeling relation.

As a result, MDD approaches place models in the core of the entire software development process. They suggest better and faster ways of developing software systems through automated model transformations that are specified with well-defined modeling languages. As a final remark, due to the fact that different MDD tools apply the same principles, an MDD expert can easily combine different approaches and tools to carry out an MDD process [Bézivin 2005]. For example, MDA concepts such as PIM and PSM metamodels can be defined with the MIC tool suite [ISIS 1997] and GME [Emerson et al. 2004]. The next section extends the MDD concepts for M&S and Section 5 presents the resulting MDD4MS framework.

#### 4. APPLYING MDD IN M&S

A simulation model is a representation of a system that can be simulated by means of experimentation [Kleijnen 2008]. It may be a physical model, a mathematical model, a computer model, or a combination of these [Roberts et al. 1983]. A simulation model is executed on a simulation platform to generate simulation results. Following the earlier definitions we say that modeling for computer simulation is the process of representing a system for a specific purpose in a form that is executable by a simulator. Figure 4 shows the basic concepts and relations based on the general modeling principles given in Section 3.1.

The main difference from a general modeling process is that the model is interpreted (i.e. executed) by a model interpreter (i.e. simulator). In the context of computer sim-

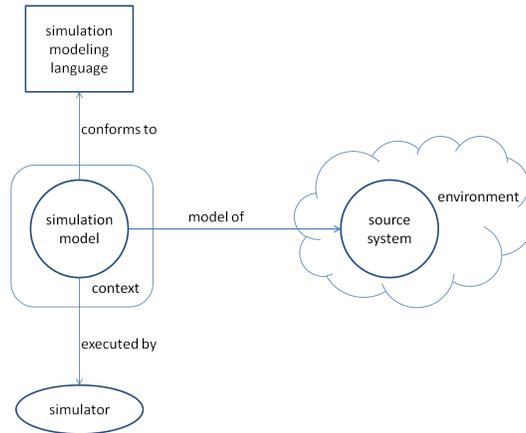


Fig. 4. Modeling and simulation in general.

ulation, a simulator is a computer program that can be executed on a computer or embedded in hardware. The output of the simulator is called the simulation results. A computer simulation model needs to be specified in a programming language that provides or can be extended to provide simulation capabilities (preferably with a suitable model editor). Simulation is the process of conducting experiments with a model so that the behavior of the system is simulated over time. We propose the following definitions based on the MDD concepts from the previous section.

*Definition 4.1 (Simulation model).* Let  $m \in M$  be a model,  $s \in S$  be a source system, and  $\mu(m, s, c)$ .  $m$  is a simulation model if, and only if, there exists a simulator that can simulate  $m$  over time.

*Definition 4.2 (Simulation modeling language).* Let  $l(g)$  be a modeling language. The language  $l(g)$  is a simulation modeling language if, and only if, there exists a simulation model  $m$  such that  $\gamma(m, l(g))$ .

System specification formalisms can be used to define simulation models in a precise way. In the M&S field, the term computer simulation model often refers directly or indirectly to the final executable source code (PSM). Hence, simulation model code generation can be perceived as a model-to-code transformation.

## 5. THEORY OF THE MDD4MS FRAMEWORK

The MDD4MS framework proposes an MDD-based simulation model development method [Çetinkaya et al. 2011]. Similar to the stages in a simulation study explained in Section 2, the MDD4MS framework addresses the steps in a simulation study from conceptual modeling through final implementation by applying metamodeling and model transformations. In this way, it can be embedded into the existing M&S methodologies easily. Appendix B presents the MDD4MS lifecycle [Çetinkaya et al. 2011; Çetinkaya et al. 2013; Çetinkaya 2013].

The MDD4MS framework introduces model and metamodel definitions for various stages, transformations between different models, methods to support the transformation steps, and a tool architecture for the overall process. When the model types in the M&S lifecycle are analyzed, it is most likely that these models need to be specified in different modeling languages. The MDD4MS framework introduces three intermediate models: a simulation conceptual model (CM), a platform independent simulation model (PISM), and a platform specific simulation model (PSSM). In addition it intro-

duces three metamodels for specifying CM, PISM and PSSM in order to support model transformations.

- . CMmetamodel represents the grammar of a conceptual modeling language,
- . PISMmetamodel represents the grammar of a system specification formalism,
- . PSSMmetamodel represents the grammar of a simulation model programming language.

CM is an instance-of CMmetamodel, PISM is an instance-of PISMmetamodel, and PSSM is an instance-of PSSMmetamodel. All of the metamodels are specified in a metamodeling language. Although it is practical to use the same metamodeling language for all metamodels, it is also possible to use different metamodeling languages as far as there is a suitable model transformation language for each transformation.

The metamodels are expected to be specified in a metamodeling environment, where model editors can be generated automatically. By using these model editors, the models are specified as the instances of the metamodels. After introducing the metamodels, the MDD4MS framework introduces model transformations between the different models of the M&S lifecycle in order to automatically generate a subset of the simulation model source code. The following metamodel-based model transformations are proposed:

- . CMtoPISM is a M2M transformation from CM to PISM.
- . PISMtoPSSM is a M2M transformation from PISM to PSSM.
- . PSSMtoSM is a M2C transformation from PSSM to SM.

Model transformations are orthogonal to metamodeling as shown in Figure 5. The figure illustrates the proposed framework with a single meta-metamodel. There are three metamodeling stacks, which are presented vertically in the figure. A practical application of the MDD4MS framework is an MDD process and it is called an MDD4MS process. Although we propose an MDD4MS process with three models and one final set of executable source code, it is possible to increase the number of models in the framework.

In the CMtoPISM and PISMtoPSSM transformations, extra information needs to be added to obtain a full model. Without extra information, either the CM should contain a full specification, which is not likely, or the target model can only be partially generated. When moving from a CM to a PISM, more detailed behavior of the system should be added, and while moving from a PISM to a PSSM, the implementation details should be added. CMtoPISM transformation contains domain specific constructs in order to add execution semantics. A PSSMtoSM transformation is generally a one-to-one transformation for a programming language and its metamodel. Defining precise metamodels and transformation rules are the challenging activities of MDD. If the modeling language is defined informally or semi-formally, which is very common for conceptual modeling languages, it is not possible to define a single and precise metamodel for that modeling language.

The expressiveness of the metamodel and the existence of component libraries are very important to be able to generate an executable and useful simulation model. Domain specific modeling languages or component libraries can be used to increase the percentage of automatically generated code. In this case, the transformations can be written in a more generic and compact way since the domain knowledge is already added via the language elements or components [Huang 2013]. In addition, higher level conceptual and platform independent models have a high potential to support efficient compositions of components developed for different environments [Diallo et al. 2011; Tolk et al. 2012; Tolk et al. 2013].

The domain-specific metamodels and model transformations need to consider the data intensive nature of simulation as well. In the MDD4MS framework, data is added on the PISM level. It is expected that the modeler will enter the data either during the CMtoPISM model transformation or add it to the PISM model itself. It is also possible that the modeler needs to manually add data into the auto-generated code. In this case, data continuity can only be guaranteed if there are parameterized components on the lowest level, and all data is entered by specifying parameter values.

MDD4MS clearly separates the conceptual modeling, model formulation (specification), implementation and model coding with the associated models CM, PISM, PSSM, and SM. However, according to the different needs in simulation projects, it is also possible to merge some stages by using the same modeling language to specify the different models, e.g., the same language can be used for CM and PISM in small scale projects. Then, the CM will be less detailed than the PISM. For example, an incomplete visual DEVS diagram can serve as a conceptual model, if the problem owner is familiar with DEVS. Besides, different model transformation patterns can be defined for a metamodel, e.g., a CM can be used to generate multiple PISMs, and a PISM can be used to generate multiple PSSMs. An implementation pattern for applying the MDD concepts in M&S domain is given as follows:

*Definition 5.1 (MDD4MS process with three models).* An MDD4MS process with three models is a specialized MDD process (Definition 3.20):

$$mdd4ms = \{n, MML, ML, MO, SL, pl, MTP, STP, MT, SM, TO\}$$

where

$$n = 3 \text{ (CM, PISM, PSSM),}$$

$MML = \{l'_0, l'_1, l'_2\}$  is an ordered set of metamodeling languages (can be defined with meta-metamodels),

$$ML = \{l_0(\text{CMmetamodel}), l_1(\text{PISMmetamodel}), l_2(\text{PSSMmetamodel})\} \text{ such that}$$

- .  $\gamma(\text{CMmetamodel}, l'_0)$ ,
- .  $\gamma(\text{PISMmetamodel}, l'_1)$ ,
- .  $\gamma(\text{PSSMmetamodel}, l'_2)$ ,

$MO = \{CM, PISM, PSSM\}$  such that CM is the initial model, PSSM is the final model, and

- .  $\tau(CM) = \text{CMmetamodel}$ ,
- .  $\tau(PISM) = \text{PISMmetamodel}$ ,
- .  $\tau(PSSM) = \text{PSSMmetamodel}$ ,

$SL$  is a set of model transformation languages,

$pl$  is a programming language with simulation capabilities,

$MTP = \{p_{cm}, p_{pism}, p_{pssm}\}$  such that

- .  $p_{cm} = \{l_0(\text{CMmetamodel}), l_1(\text{PISMmetamodel}), r_0\}$ ,
- .  $p_{pism} = \{l_1(\text{PISMmetamodel}), l_2(\text{PSSMmetamodel}), r_1\}$ ,
- .  $p_{pssm} = \{l_2(\text{PSSMmetamodel}), pl, r_2\}$ ,

$STP$  is a set of other supplementary formal model transformation patterns,

$$MT = \{(\theta(CM, p_{cm}) = PISM), (\theta(PISM, p_{pism}) = PSSM), (\theta(PSSM, p_{pssm}) = SM)\},$$

$SM$  is the final executable simulation model,

$TO$  a set of tools to ease the activities.

Finally, we propose that any practical application of the MDD4MS framework obtains model continuity.

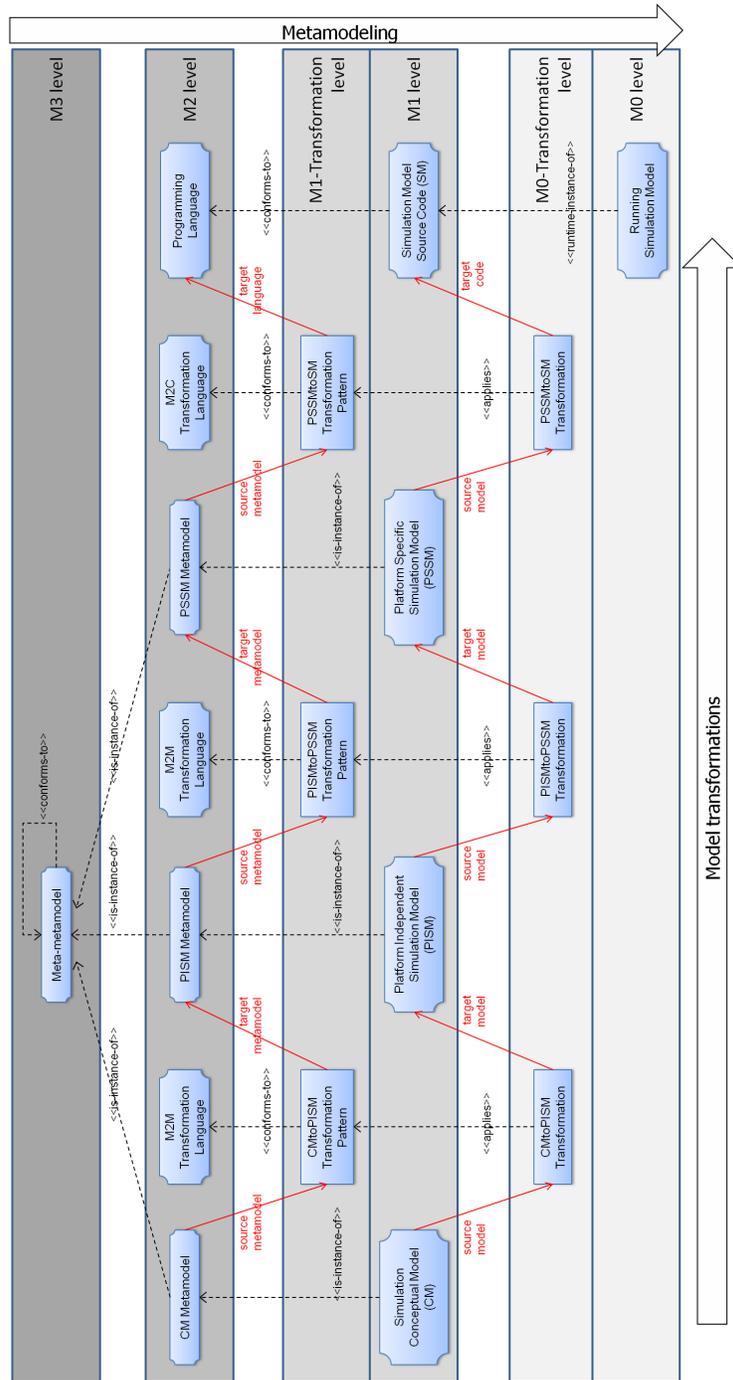


Fig. 5. MDD4MS framework: models, metamodels and model transformations [Çetinkaya 2013].

**THEOREM 5.2.** *An MDD4MS process with three models (performed according to the Definition 5.1) obtains model continuity.*

**PROOF.** For a given  $mdd4ms = \{n, MML, ML, MO, SL, pl, MTP, STP, MT, SM, TO\}$ , by definition 5.1, where  $n = 3$  and  $MO = \{CM, PISM, PSSM\}$  we have:

- .  $CM, PISM, PSSM \in M$ ,
- .  $p_{cm} = \{l_0(CMmetamodel), l_1(PISMmetamodel), r_0\}$ ,
- .  $p_{pism} = \{l_1(PISMmetamodel), l_2(PSSMmetamodel), r_1\}$ ,
- .  $p_{pssm} = \{l_2(PSSMmetamodel), pl, r_2\}$
- .  $\theta(CM, p_{cm}) = PISM$ ,
- .  $\theta(PISM, p_{pism}) = PSSM$ ,
- .  $\theta(PSSM, p_{pssm}) = SM$ ,
- .  $SM$  is the final executable simulation model.

We assume that  $CM$  is the initial model,  $\mu(CM, s, c)$  and  $s$  is a system. Although,  $PSSM$  is the final model in software engineering, we accept that  $SM$  is the final model in M&S.

- (1)  $(\theta(CM, p_{cm}) = PISM) \wedge \mu(CM, s, c) \wedge PISM \in M \Rightarrow \mu(PISM, s, c + p_{cm})$   
(by theorem 3.14).
- (2)  $(\theta(PISM, p_{pism}) = PSSM) \wedge \mu(PISM, s, c + p_{cm}) \wedge PSSM \in M \Rightarrow$   
 $\mu(PSSM, s, c + p_{cm} + p_{pism})$  (by 1 and theorem 3.14).
- (3) If  $SM$  is a simulation model, then  $SM \in M$  (by definition 4.1).
- (4)  $(\theta(PSSM, p_{pssm}) = SM) \wedge SM \in M \wedge \mu(PSSM, s, c + p_{cm} + p_{pism}) \Rightarrow$   
 $\mu(SM, s, c + p_{cm} + p_{pism} + p_{pssm})$  (by 1, 2, 3 and theorem 3.14).
- (5)  $n \geq 2 \wedge \mu(SM, s, c + p_{cm} + p_{pism} + p_{pssm}) \Rightarrow mdd4ms$  process obtains model continuity  
(by definition 3.21).

□

The next section presents an overview of a case study to apply MDD4MS in the discrete event simulation domain.

## 6. PROOF OF CONCEPT: DISCRETE EVENT SIMULATION OF BPMN MODELS

To show the applicability of the MDD4MS process, we have chosen a sample problem from the electronic payments sector which is presented in [Sun et al. 2009]. The crucial role of M&S within this example is to document the business processes as much as possible in a visualized way, to enable different parties to gain insight into the issues and into potential solutions. A manually developed simulation model is available [Sun et al. 2009] for comparison with our auto-generated model. We used the MDD4MS prototype implementation to develop the simulation model [Çetinkaya et al. 2013]. The MDD4MS prototype implementation is an Eclipse-based application of the MDD4MS tool architecture, which is defined in the MDD4MS framework [Çetinkaya et al. 2011].

We used BPMN (Business Process Model and Notation) for conceptual modeling, DEVS for system specification and Java for the simulation model code. Please note that these languages are used just to provide a proof of concept implementation. They are not part of the MDD4MS framework and any other conceptual modeling language, system specification language, or simulation model programming language could have been chosen. For example, UML activity diagramming technique could be used as conceptual modeling language; Petri Nets could be used as system specification language; and C++ could be used as simulation model programming language. In this case, new metamodels and transformation rules would have to be developed.

According to the MDD4MS framework, the following metamodels and model transformations are needed:

- . BPMN metamodel as the CMmetamodel,
- . DEVS metamodel as the PISMmetamodel,
- . JAVA metamodel as the PSSMmetamodel,
- . BPMNtoDEVS transformation as the CMtoPISM transformation,
- . DEVStoJAVA transformation as the PISMtoPSSM transformation,
- . JAVAtoJAVACode transformation as the PSSMtoCode transformation.

*Definition 6.1 (MDD4MS case example).* Model driven development of DEVS-based simulation models from BPMN models is an MDD4MS process defined as

$$case = \{n, MML, ML, MO, SL, pl, MTP, STP, MT, SM, TO\}$$

where

$$n = 3 (CM, PISM, PSSM),$$

$MML = \{Ecore, Ecore, Ecore\}$  is the ordered set of metamodeling languages,

$ML = \{l_0(BPMNmetamodel), l_1(DEVSmetamodel), l_2(JAVAmetamodel)\}$  such that

- .  $\gamma(BPMNmetamodel, Ecore)$ ,
- .  $\gamma(DEVSmetamodel, Ecore)$ ,
- .  $\gamma(JAVAmetamodel, Ecore)$ ,

$MO = \{CM, PISM, PSSM\}$  such that CM is the initial model, PSSM is the final model, and

- .  $\tau(CM) = BPMNmetamodel$ ,
- .  $\tau(PISM) = DEVSmemodel$ ,
- .  $\tau(PSSM) = JAVAmetamodel$ ,

$SL = \{ATL, JAVA\}$  is the set of model transformation languages,

$pl = JAVA$  is the programming language and it is extended with simulation libraries,

$MTP = \{p_{cm}, p_{pism}, p_{pssm}\}$  such that

- .  $p_{cm} = \{l_0(BPMNmetamodel), l_1(DEVSmetamodel), bpmn2devs.atl\}$ ,
- .  $p_{pism} = \{l_1(DEVSmetamodel), l_2(JAVAmetamodel), devs2java.atl\}$ ,
- .  $p_{pssm} = \{l_2(JAVAmetamodel), JAVA, java2code.java\}$ ,

$STP = \{\}$  is the set of other supplementary formal model transformation patterns,

$MT = \{(\theta(CM, p_{cm}) = PISM), (\theta(PISM, p_{pism}) = PSSM), (\theta(PSSM, p_{pssm}) = SM)\}$ ,

$SM$  is the final executable simulation model,

$TO = \{Eclipse \text{ and a set of plugins}(GEMS, ATL, PDE, EMF, GEF)\}$  is the set of tools to support the activities.

The MDD4MS prototype implementation includes metamodels, model editors, model transformation rules, and model interpreters for DEVS-based simulation of BPMN models [Çetinkaya et al. 2013; 2012; 2011]. The BPMNtoDEVS transformation produces atomic and coupled models with ports, couplings and templates for the system behavior. The DEVStoJAVA transformation produces valid Java visual models with information for Java classes. The JAVAtoJAVACode transformation generates Java code. In order to support the transformation process and to generate fully executable DEVS models, a DEVS simulation model component library for BPMN was used [Rust et al. 2011]. By using validated DEVS components, which are implemented in Java and executable with the DEVSDSOL simulation library, we ensured that the semantics of the DEVS model was preserved in the Java model. The case example showed that model continuity between the different models within the M&S lifecycle was obtained when

the MDD4MS framework is applied. The metamodels specified in Ecore [Eclipse 2014] and more information about the case study can be found in Appendix C.

## 7. CONCLUSIONS

Applying MDD in M&S provides new capabilities for efficient development of reliable, error-free and maintainable simulation models. Availability of tools and techniques for both metamodeling and model transformations is one of the practical advantages of MDD. Metamodeling provides a precise way for specifying models and their modeling languages.

This paper proposes a comprehensive theoretical framework for model driven development of simulation models. The framework recommends the use of three intermediate models in addition to the executable simulation model. We showed that the proposed MDD4MS framework obtains model continuity via formal, metamodel-based model-to-model transformations. The main objective of this research was to improve and speed-up the simulation model development process by using software engineering methods. The most important outcomes of applying MDD in the M&S domain are: providing syntactic and semantic validity of the models, formalizing the modeling steps and the process, increasing productivity, and providing model continuity.

The case study illustrated that the framework is applicable in the DEVS-based discrete-event simulation domain. Due to the fact that there are other successful studies on applying MDD and component-based approaches in the simulation field, and because MDD4MS provides a generic framework, we believe that MDD4MS is also applicable in other domains. Future work will therefore include testing the MDD4MS framework in different domains and in large scale real life M&S studies. In the presented case study, there was still some work for the modeler, e.g., adding data during the CMtoPISM model transformation, and selecting appropriate components during the PISMtoPSSM model transformation. Further research will study possible extensions to the framework to be able to select automatically among alternatives at various levels and testing the quality of these choices.

MDD is different from traditional development approaches and it requires a learning period and change of standard M&S development habits. When modeling languages for the different stages are not yet available and the team members have little or no knowledge about MDD, it may take quite some time to develop metamodels and model transformations. However, once these are developed, further development time and costs decrease significantly. A model-driven approach is therefore expected to have most benefits for multiple projects in the same domain, and for large-scale and critical simulation projects.

## ELECTRONIC APPENDIX

The electronic appendix for this article can be accessed in the ACM Digital Library.

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