1	Effects of particle size on the separation efficiency in a rotary-drum
2	eddy current separator
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14	Abstract: Eddy current separation is a technology for recovering non-ferrous metals.
15	The influence of particle size on the separation is of significant importance due to the
16	variety of materials. It was investigated by combining simulations and physical
17	experiments. A strong correlation between the simulation and the experiment was
18	found by Pearson correlation analysis. Then the interaction effects between the
19	particle size and the material type, rotational speed, magnetic pole arrangement were
20	investigated. It shows that an optimal particle size exists for a specific condition, and
21	the separation efficiency of fine particles can be improved by increasing rotational
22	speed, magnetic pole number, and the electrical conductivity/density of material, as

well as utilizing torque of Lorentz force. The underlying mechanism of particle size
affecting separation was discovered by analyzing eddy current distribution and field
gradient. These results provide insight into the design and optimization of eddy
current separation for particles of various sizes.

Keywords: Particle size; eddy current separation; numerical simulation; Lorentz force;
magnetic dipole

29 **1. Introduction**

Solid waste recycling has become one of the most important processes to the 30 31 environmental protection and the sustainable use of resources and energy [1]. Furthermore, the recovery of metallic components in solid wastes is of great 32 economic value, which has attracted increasing attention worldwide. In the metal 33 34 recovery process, mechanical and physical separation methods such as optical separation, gravity separation, and electromagnetic separation are usually used to 35 complete the upgrading process of various materials before the refining operation [2]. 36 37 Optical separation methods can be used for the separation of various material types [3], but they are usually only suitable for mixtures with large particle size (>10 mm), 38 and the equipment is also relatively expensive. Gravity separation methods are 39 suitable for materials with sufficiently differences in density or particle size [4]. 40 Electromagnetic separation methods, mainly including electrostatic separation [5], 41 magnetic separation [6] and eddy current separation, are capable of processing 42 mixtures with a wide range of particle sizes, appropriate for a wide variety of solid 43 wastes. The last two are usually used together on the same production line: the 44

ferromagnetic metals are separated from the mixture by magnetic separator, and then
non-ferrous metals and non-metallic materials are separated by eddy current separator
(ECS) [7].

In ECS, Lorentz force (F_{eddy}) is responsible for separating non-ferrous metal 48 particles from other materials [8]. There are two recognitions for the Lorentz force in 49 eddy current separation: (1) the eddy current in the conductive particle is induced 50 under the alternating magnetic field, and the eddy current further interacts with the 51 alternating magnetic field to generate a repulsive force; (2) the alternating magnetic 52 53 field induces eddy current in the conductive particle, and the derived magnetic field generated by the eddy current interacts with the alternating magnetic field to form a 54 repulsive force. The theoretical models were developed based on the above two 55 56 recognitions respectively [9]. This technology has the advantages of low energy consumption, large processing capacity, easy operation, and no secondary pollution. It 57 is the most suitable separation technology for large-scale recycling of non-ferrous 58 59 metals [9], and has been widely used to process various mixtures including the electronic waste [10], incinerator bottom ash [11], automotive shredder residue, 60 foundry sand, etc [12]. Moreover, some researchers are also trying to use the principle 61 of ECS to manipulate and clean up the space debris [13]. Despite the advantages 62 63 mentioned above, the ECS suffers poor separation efficiency for mixtures consisting of fine particles (<5 mm), significantly restricting the further development of eddy 64 65 current separation technology [8]. Improving the separation efficiency of mixtures with various particle sizes in ECS can create a considerable deal of social and 66

economic benefits. For example, more than 10 million tons of bottom ash, containing 67 5-8% metals, are generated annually in China through the incineration of municipal 68 69 solid waste. Around 78% of the Cu present in the bottom ash with a particle size of less than 5 mm, which is directly discarded due to the poor separation efficiency of 70 71 the ECS [14]. As another example, electronic wastes need to be crushed to achieve the 72 liberation of various materials like metals and plastics before the separation. The statistical results show that when the printed circuit boards are crushed below 6 mm, 73 ferromagnetic particles and Cu can be completely liberated [15]. Therefore, the 74 75 effective separation of the fine particles is key to recycling electronic wastes.

To solve the challenges associated with the low separation efficiency of ECS for 76 fine particles, some researchers have suggested increasing the Lorentz force by 77 adjusting the intensity and frequency of the alternating magnetic field. 78 High-frequency electromagnetic ECS (50~100 kHz) was used to separate fine 79 particles [16]. The recovery rate of Al, Cu, and Zn particles (0.8~4 mm) could exceed 80 81 the value of 85% under appropriate parameters. Despite the desirable outcomes, the utilization of such equipment at large scales is challenging, due to the fact that the 82 mixture is separated in a narrow air gap, with a processing capacity of 50 kg/h [17]. A 83 superconducting ECS [18] with a center field intensity of up to 5 T has also been 84 suggested to increase the efficiency of the process, but the separation effect is yet to 85 be confirmed by experiments. Another approach is based on the rotational motion 86 generated by the torque of Lorentz force (T_{eddy}) to achieve the separation of fine 87 particles. This is known that the rotational angular velocity of small non-ferrous metal 88

particles in an alternating magnetic field can reach about 1000 rad/s [19]. Therefore, 89 when the rotating particle pass through fluids such as air, the particle trajectory is 90 91 affected by the Magnus force [20], resulting in additional deflection. The separation of non-ferrous metal particles in air and water was studied by employing this 92 mechanism [21]. It was found that the Magnus effect can increase the recovery rate 93 and grade of Cu particles by about 4%. In addition, a bottom-feeding ECS was 94 proposed [22]. In this type of ECS, the non-ferrous metal particles are affected by the 95 torque of Lorentz force, causing the non-ferrous metal particles to roll forward and 96 97 jump, which is helpful to improve the separation of fine particles. However, the utilization of torque of Lorentz force is susceptible to the influence of particle shape, 98 thus the grade and recovery rate of separation are low, limiting the industrial 99 100 applications of these techniques. Other researchers tried to reduce the critical conditions required to achieve the separation through the implementation of smart 101 structures and process arrangements. For example, the single-disk ECS requires only 102 103 a short jump of non-ferrous metal particles under the action of Lorentz force to achieve effective separation [23]. Moreover, when feeding mixtures with high 104 humidity in a traditional belted-drum ECS. The Lorentz force only needs to be greater 105 than the adhesion force between the particles and the belt, or the liquid bridge can be 106 broken by the rotation motion of the particles, to achieve effective separation [19]. 107 However, the processing capacity of these ECS is small, and the industrial application 108 109 of such complicated devices can be challenging.

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At present, the structure that the market still favors is the traditional belted-drum

ECS [8]. In the belted-drum ECS, the research on particle size mostly adopts the 111 research method of separation experiment. These studies have clarified the influence 112 113 of particle size on repulsion distance (D_r) [24], grade, and recovery rate [25], but the underlying mechanisms governing the separation are still unclear, which is an 114 important reason for the low separation efficiency of fine particles. To better 115 understand the mechanisms by which the particle size affecting the separation, the 116 electromagnetic and dynamic responses of non-ferrous metal particles should be 117 investigated. In ECS, the trajectories of non-ferrous metal particles are simultaneously 118 119 affected by Lorentz force and torque, gravity, aerodynamic drag force, Magnus effect, etc. And the dynamic variation of eddy current in non-ferrous metal particles is 120 complicated. It is difficult to observe or measure the electrodynamic behavior of 121 122 non-ferrous metal particles in separation experiments, so some researchers used numerical simulations. Bin et al. [26] studied the relationship between the magnetic 123 roller structure and the distribution characteristics of the magnetic field based on finite 124 125 element analysis (FEA). Huang et al. [27] proposed that there is no size limitation for the non-ferrous metals in eddy current separation by simulating and analyzing the 126 magnetic field of magnetic poles based on FEA. Zhang et al. [28] studied the 127 influence of particle size on the repulsion distance through an iterative simulation 128 model based on the magnetic dipole theory. Ayad et al. [29] used a 2D simulation 129 model based on FEA to study the effects of conductivity and particle size on the 130 Lorentz force and eddy current. However, these simulation models use simplified 2D 131 geometric model, or ignore the effect of torque of Lorentz force, and do not establish 132

a relationship between the separation efficiency indicator and the physical quantities 133 in the simulation. A three-dimensional transient simulation model of ECS has been 134 established and verified in our previous research on material temperature [30]. It can 135 provide more detailed information such as Lorentz force and torque, eddy current, etc. 136 In this study, the relationship between several key physical quantities in the 137 numerical simulation and separation experiment was analyzed. On this basis, the 138 influence of particle size on the separation efficiency and the related mechanisms 139 were further studied. The research results can provide guidance for the design and 140 141 optimization of eddy current separators.

142

2. Materials and methods

To systematically evaluate the impact of particle size on separation efficiency in eddy current separation, the combination of numerical simulation and experiment was used in this study. This section describes in detail the numerical simulation model and the separation experimental process.

147 2.1 Three-dimensional transient simulation model of ECS

In this study, a self-designed rotary-drum ECS (Fig. 1 (a)) was used as a prototype, and the corresponding three-dimensional transient simulation model of ECS was built based on FEA, as shown in Fig. 1 (b). The rotary-drum ECS is mainly composed of a magnetic roller, an electric motor, a control cabinet, and a frame. It is simplified as a rotating magnetic roller structure including an iron core and permanent magnets in the simulation model to ensure that the computational workload and accuracy of the numerical simulation are within a reasonable range. The magnetization direction of the red permanent magnet (N pole) on the magnetic roller is radially outward, while the magnetization direction of the light green permanent magnet (S pole) is radially inward. N52 grade permanent magnets were used. There are two magnetic pole arrangements of NNSS and NS set on the magnetic roller in the simulation model, which is consistent with that in the rotary-drum ECS.

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Fig. 1. (a) The rotary-drum ECS; (b) the three-dimensional transient simulation model
of ECS; (c) the feeding pipe and non-ferrous metal particles for physical experiment.
Solving an electromagnetic field problem is always based on solving Maxwell's
equations. However, the process of obtaining the solution is typically based on
solving a second order consequence of Maxwell's equations with the consideration of
applicable constitutive equations. The following constitutive relationship is relevant

168 for the magnetic field of the magnetic poles:

$$\vec{B} = \mu_0 \left(\vec{H} + \vec{M} \right) \tag{1}$$

170 where $\vec{B}(x, y, z)$ is the magnetic flux density. $\vec{H}(x, y, z)$ is the magnetic field 171 strength. $\vec{M}(x, y, z)$ is the permanent magnetization. $\mu_0 = 4 \cdot \pi \cdot 10^{-7} H/m$ is the 172 permeability of vacuum. The component of the Lorentz force due to current in a 173 magnetic field is given by the following equation:

174
$$\mathbf{F}_{eddy} = \int_{V} J \times BdV \tag{2}$$

where J is the current density, and V is the volume of the particle. The system uses Lorentz forces to compute the torque around each axis, and the torque of Lorentz force on the particle is:

178
$$T_{eddy} = \int_{V} \gamma \times (J \times B) dV$$
(3)

179 where γ is the displacement vector from the rotation axis.

In the simulation model, the rotational speed of the magnetic roller can be 180 adjusted according to the design. The frequency of the magnetic field around the 181 182 magnetic roller increases with the increase of rotational speed. Non-ferrous metal particles with different sizes are set to be next to the rotating magnetic roller, so that 183 the electrodynamic state of the non-ferrous metal particles in an alternating magnetic 184 field can be simulated. The master-slave boundary condition is adopted on the two 185 ends of the magnetic roller in the axial direction, which can eliminate the error caused 186 by the end effect of the magnetic roller, thus greatly reduce the axial length of the 187 magnetic roller in the simulation model. In addition, some parameters such as the time 188 step and circumferential boundary used in the simulation model were determined by 189

the independence verification. The simulation model can be used to obtain the 190 physical quantities such as eddy current, Lorentz force and torque of the non-ferrous 191 metal particles near the rotating magnetic roller under different conditions. It should 192 be noted that the simulation model in this study does not include the effects of gravity 193 and aerodynamic drag forces. The premise of studying these forces is to achieve the 194 coupling of finite element analysis and computational fluid dynamics, which will be 195 the focus of our future work. The specific geometric structure and simulation 196 parameters are shown in Table 1. 197

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Table 1. Parameters used in the simulations.

Catego	bry	Values
Permanent magnet	Inner radius (mm)	98
	Outer radius (mm)	138
	Height (mm)	70
	Magnetic pole pairs	9
	Remanence (T)	1.43
Back iron	Inner radius (mm)	68
	Outer radius (mm)	98
	Height (mm)	70
	Relative permeability	4000
Non-ferrous metal particle	Particle size (mm)	1-32
Rotational speed of roller (rpm)		1200-6000
Time step (ms)		0.01-0.05

199 2.2 Separation experiment method

200 The separation experiment was also carried out to clarify the relationship

between the Lorentz force in the simulation and the repulsion distance in the separation experiment. The rotary-drum ECS was used to carry out the separation experiments under different particle sizes, material types and rotational speeds. The specific experimental parameters are shown in Table 2.

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Table 2. Parameters used in the experiments.

Material type	Rotational speed (rpm)	Particle size (mm)
Al	1800	3, 4, 5, 6, 7, 8
	3000	3, 4, 5, 6, 7, 8
Brass	3000	3, 4, 5, 6, 7, 8

In eddy current separation, particle motion includes translational motion and 206 rotational motion. Since the Lorentz force is proportional to the magnetic flux area, 207 the trajectories of particles with asymmetric shapes are affected by their own shapes 208 and have stronger randomness, so spherical particles were used in the separation 209 210 experiments. Al and brass, which are the most common non-ferrous ingredients of industrial solid wastes, were used. To minimize the influence of the initial state of 211 particles on the results of the separation experiment, feeding pipes with the same 212 213 length and different tube diameters were set in the feeding area, and the non-ferrous metal particles of various sizes pass through the feeding pipe before entering the 214 separation area. The particles with diameters of 3-8 mm were matched with the 215 feeding pipes with tube diameters of 4-9 mm and wall thickness of 1 mm, as shown in 216 Fig. 1 (c). Feeding pipes were used to reduce random errors caused by the manual 217 operation during feeding, so that particles of different sizes and materials can maintain 218 a relatively consistent initial movement state and spatial position before entering the 219 separation area. The non-ferrous metal particles are deflected by the Lorentz force and 220

torque in the separation area. There are some pre-set scale marks in the landing area, 221 and the whole process was filmed at 60 Hz by a video camera, and then the repulsion 222 223 distance can be measured by analyzing the film frame by frame. The separation experiments under the same experimental condition were repeated at least 15 times, 224 which can further reduce the experimental error. The experimental data of these 225 repulsion distances meet the characteristics of normal distribution. And the average 226 value represents the distance that the non-ferrous metal particles are thrown out by the 227 Lorentz force, so it can directly reflect the separation efficiency between non-ferrous 228 229 metal particles and non-metallic particles [24]. The standard deviation of the repulsion distance represents the concentration of the particle falling points, which is very 230 critical when evaluating the separation effect between different non-ferrous metals. 231

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3. Results and discussion

233 3.1 Correlation between simulations and separation experiments

In the simulations, many physical quantities that are difficult to measure in the 234 235 separation experiments can be relatively easily obtained. However, when applying the simulation model, the connection between several key physical quantities in the 236 simulation and separation experiment should be established to ensure that some 237 quantities in the simulation model have physical meaning. Lorentz force is the power 238 source that drives the non-ferrous metal particles to move in translation and deviate 239 from other materials, so it is a very critical physical quantity in the eddy current 240 separation. In the separation experiment, the Lorentz force is difficult to measure, but 241 the specific value of the Lorentz force can be obtained conveniently in the simulation. 242



Fig. 2. The effect of particle size on the translational motion: the variation of average Lorentz force, average direction angle (a) and average acceleration (b) of Al particle with particle size when the rotational speed is 3600 rpm

Fig. 2 (a) shows the variation of the average Lorentz force $(\overline{F_{eddy}})$ and the average direction angle $(\overline{\theta})$ of Al particles with the particle size when the rotational speed is 3600 rpm. It shows that the increase of $\overline{F_{eddy}}$ spans several orders of magnitude with the increase of particle size. Therefore, a semi-logarithmic scale is used in the vertical axis on the left in the figure. This indicates that particle size is one of the most important factors affecting the Lorentz force. In fact, the dependence of

the Lorentz force on the particle size is an important reason for the difficult separation 253 of fine particles. The direction angle (θ) of the Lorentz force will also has a greater 254 255 impact on the particle trajectory, but no study has concerned this issue so far. In a common belted-drum ECS, non-ferrous metal particles enter the separation area along 256 the circumferential direction of the magnetic roller surface, and the particles do the 257 projectile motion under the action of Lorentz force. When the Lorentz force is 258 constant, the closer the direction angle is to 45°, the greater the repulsion distance of 259 the non-ferrous metal particles [31]. For the vertical rotary-drum ECS, the non-ferrous 260 261 metal particles enter the separation area along the generatrix direction of the magnetic roller surface, and the particles do horizontal throwing motion when subjected to the 262 Lorentz force. In this case, the direction angle also has a direct impact on the radial 263 264 repulsion distance and the circumferential deflection of the non-ferrous metal particles. When the Lorentz force is constant, the closer the direction angle is to 90°, the greater 265 the repulsion distance of non-ferrous metal particles. Fig. 2 (a) shows that the 266 267 direction angle of the Lorentz force also increases with the increase of the particle size, which also explains the low separation efficiency of small particles. This may be 268 because the magnetic field gradient in the radial direction near the surface of the 269 magnetic roller is larger than that in the tangential direction, and the magnetic field 270 271 gradient is closely related to the magnitude of the Lorentz force [32]. In this case, when the particle size increases, the radial Lorentz force (F_{radial}) increases more than 272 the tangential Lorentz force ($F_{tangential}$), and the direction angle of the Lorentz force 273 increases accordingly. 274



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Fig. 3. The effect of particle size on the rotational motion: (a) the variation of the torque of Lorentz force of aluminium particle (8 mm) with time under the rotational speed of 3600 rpm; (b) the variation of the average torque of Lorentz force and its angular acceleration with the particle size at 3600 rpm.

The translational motion of non-ferrous metal particles with different particle sizes under Lorentz force is also related to their own mass. Thus the acceleration of particles by Lorentz force was investigated to eliminate the interference of the particle mass. Fig. 2 (b) shows the variation of the acceleration of $\overline{F_{eddy}}$ on the Al particle

with the particle size under the rotational speed of 3600 rpm. It shows that when the 284 particle size increases, the acceleration of non-ferrous metal particles does not 285 286 increase continuously like the Lorentz force. Instead, a peak was observed when the particle size is about 19 mm in this case. This indicates that there may be an optimal 287 separation particle size under specific structural parameters and operating parameters. 288 These results are consistent with the changing trend of the repulsion distance based on 289 an analytic model [33], which shows that the acceleration of Lorentz force can better 290 291 reflect the actual separation effect than Lorentz force.

292 When dealing with the problem of difficult separation of fine particles, the torque of Lorentz force causing the rotational motion of non-ferrous metal particles 293 has gradually attracted attention in the design of some new eddy current separator [8]. 294 295 Fig. 3 (a) shows the variation of torque of Lorentz force components on an 8 mm diameter Al particle with time at 3600 rpm. The x, y, and z in the figure are the three 296 axes of the local coordinate system with the origin at the particle center, and T_{eddy}^{x} , 297 T_{eddv}^{y} , and T_{eddy}^{z} are the components of torque of Lorentz force in the triaxial 298 direction respectively. It shows that the component of torque of Lorentz force about 299 the x and y axes is almost zero, while the component of torque of Lorentz force about 300 the z axis fluctuates with time. The large fluctuations correspond to the magnetic pole 301 302 of NNSS, while the small fluctuations correspond to the magnetic pole of NS. This indicates that the fluctuates of T_{eddy}^{z} are due to the change of magnetic field 303 distribution caused by the alternating structure of N and S poles in the circumferential 304 direction of the magnetic roller. Meanwhile, there is no structural change in the axial 305

direction of the magnetic roller, and the magnetic field is evenly distributed in the axial direction. The axial Lorentz force on the internal parts of the non-ferrous metal particle is almost zero, so the components of the torque of Lorentz force on the x and y axes are also close to zero, as expected. Similar phenomena can be found when investigating the variation of each component of torque of Lorentz force with time under other conditions. Thus T_{eddy}^{z} can be used as an accurate approximation for the total torque acting on the particle.

When studying the actual effect of the torque of Lorentz force on the rotational 313 314 motion of the particles, it is necessary to eliminate the influence of the moment of inertia. Fig. 3 (b) shows the variation of average torque of Lorentz force $(\overline{T_{eddy}^z})$ and 315 the corresponding angular acceleration (α) with particle size. The angular acceleration 316 can be calculated according to $\overline{T_{eddy}^{z}} = I\alpha$, where I is the moment of inertia of the 317 particle about an axis through the particle center. It shows that the average torque of 318 Lorentz force increases with the increase of the particle size, and the angular 319 320 acceleration corresponding to the average torque of Lorentz force decreases with the increase of the particle size. The results indicate that when the particle size decreases, 321 the reduction rate of the moment of inertia is higher than that of the torque of Lorentz 322 force, so the angular acceleration representing the intensity of the rotational motion 323 324 has a continuous strengthening trend. Thus it can be seen that the torque of Lorentz force can be used to improve the separation efficiency of fine particles. These results 325 326 can also be used to explain why the reversal of the magnetic roller can improve the separation efficiency of fine particles [34]. We should pay attention to the role of 327

particle rotation when designing ECS for fine particles. Combining with the results of Fig. 2, it can be found that the Lorentz force and torque of non-ferrous metal particle increase significantly by 6 orders of magnitude with the increase of particle size. However, the increase of particle size will also cause the changes in mass and moment of inertia, so the acceleration and angular acceleration of particle can more directly reflect the translational and rotational motion of particles.



Fig. 4. Relationship between the simulation and the separation experiment under different particle sizes, material types and rotational speeds: (a) the relationship between the acceleration of $\overline{F_{eddy}}$ and the average repulsion distance; (b) the

relationship between the standard deviation of Lorentz force and the standard

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deviation of repulsion distance.

The relationships between the physical quantities in the simulation and the actual 340 separation effect were investigated to justify the physical meaning of some quantities 341 in the simulation and further verify the accuracy of the simulation model. The 342 equipment used in the separation experiment is a vertical rotary-drum ECS, which 343 achieves the separation based on the translational motion of non-ferrous metal 344 particles caused by Lorentz force. Thus the relationship between the Lorentz force and 345 346 the repulsion distance was investigated. The simulations and separation experiments included in Fig. 4 adopted the same experiment parameters (see Table 2 presented 347 earlier in section 2.2), and Table 3 is the Pearson correlation analysis and linear 348 349 regression analysis results corresponding to Fig. 4. Fig. 4 (a) is the relationship between the average repulsion distance $(\overline{D_r})$ in the separation experiments and the 350 acceleration of $\overline{F_{eddy}}$ in the simulations. It shows that there is a linear correlation 351 between the average repulsion distance and the acceleration of $\overline{F_{eddy}}$ on non-ferrous 352 metal particles under the same material type and rotational speed, and the trend lines 353 of the same material type almost overlap each other. The results indicate that the 354 acceleration of $\overline{F_{eddv}}$ is closely related to the average repulsion distance, so the 355 acceleration of $\overline{F_{eddy}}$ is the key factor affecting the repulsion distance. It can be used 356 to evaluate the separation effect between non-ferrous metals and non-metals just like 357 the repulsion distance: The greater the acceleration of $\overline{F_{eddy}}$, the better the separation 358 effect between non-ferrous metals and non-metals. Fig. 4 (b) is the relationship 359

between the standard deviation of the repulsion distance in the separation experiments 360 and the standard deviation of the Lorentz force in the simulations. Similarly, there is a 361 linear correlation between the standard deviation of the repulsion distance and the 362 standard deviation of the Lorentz force, and the trend lines of the same material type 363 almost overlap each other. The results show that the standard deviation of Lorentz 364 force can characterize the concentration degree of particle falling points as the 365 standard deviation of repulsion distance. Therefore, the standard deviation of Lorentz 366 force can be used as a reference value in evaluating the separation effect between 367 different non-ferrous metals. 368

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Table 3. Correlation and linear regression analysis for the relationship between

simulations and physical experiments.

Category	Material type	Rotational speed	R ²	Correlation
		(rpm)		coefficient
Analysis on $\overline{D_r}$ and	Al	1800	0.9988	0.9994
acceleration of		3000	0.9973	0.9986
$\overline{F_{eddy}}$, Fig. 3(a)	Brass	3000	0.9947	0.9973
Analysis on the	Al	1800	0.9341	0.9665
standard deviation		3000	0.8864	0.9415
for D_r and F_{eddy} , Fig. 3(b)	Brass	3000	0.9583	0.9789

371	The coefficient of determination (R^2) measures the fraction of the total variation
372	in the dependent variable that is explained by the independent variable. The values of
373	R^2 in Table 3 are all greater than 0.85, which indicates that the acceleration and
374	fluctuation of the Lorentz force can explain most of the variation in the mean and
375	standard deviation of the repulsion distance. The order of R^2 in Fig. 4 (b) is: 3000
376	rpm-Al<1800 rpm-Al<3000 rpm-Brass, which is mainly determined by the magnitude

of the standard deviation of each group of experiments. For example, the standard 377 deviation of the Lorentz force and the repulsion distance of the Al particle at 3000 378 379 rpm is the largest, then the randomness of this set of data is the largest, so the variation caused by random factors is also the largest. In addition, Table 3 shows that 380 the correlation coefficients between physical quantities in the separation experiments 381 and simulations are all greater than 0.94, reaching a very high degree of correlation. 382 The results in Fig. 4 and Table 3 prove the physical meaning of the acceleration and 383 standard deviation of the Lorentz force in the simulation, and also verify the accuracy 384 385 of the three-dimensional transient simulation model of ECS. On this basis, a more detailed study on particle size can be carried out by using the simulation model. 386 3.2 The interaction effects between particle size and other factors 387

388 The major choke point of the eddy current separation technology is the low 389 separation efficiency of fine particles. Studying the interaction effects between the 390 material parameters (material type), operating parameters (rotational speed), structural 391 parameters (magnetic pole arrangement) and the particle size can guide the design, 392 optimization and process of eddy current separator for fine particles.



Fig. 5. The influence of the interaction effects on the acceleration of $\overline{F_{eddy}}$: (a) the variation of the acceleration of $\overline{F_{eddy}}$ on Al and brass particles with particle size when the rotational speed is 6000 rpm; (b) the acceleration of $\overline{F_{eddy}}$ on Al particle varies with particle size at different rotational speeds; (c) the variation of the

acceleration of $\overline{F_{eddy}}$ on Al particle with particle size under the two magnetic pole arrangements at a rotational speed of 6000 rpm.

Fig. 5 shows the influence of the interaction effects between the particle size and 400 the material type, rotational speed, and magnetic pole arrangement on the acceleration 401 of $\overline{F_{eddy}}$. It shows that the acceleration of $\overline{F_{eddy}}$ under various experimental 402 conditions has a peak value, which corresponds to an optimal separation particle size. 403 Thus the particle size range of the target mixture should be investigated before 404 designing or optimizing the ECS, and then the parameters suitable for separating the 405 mixture should be set according to the particle size range. Fig. 5 (a) shows the 406 variation of the acceleration of $\overline{F_{eddy}}$ on Al and brass particles with particle size 407 under the rotational speed of 6000 rpm. The ratio of electrical conductivity to density 408 (σ/ρ) is an important indicator for evaluating material differences in eddy current 409 separation, and the σ/ρ of Al and brass are 12.96 and 2.44, respectively [1]. It can 410 be seen that the interaction effect between particle size and material type is significant. 411 When the σ/ρ of the material is large, the particle size has a greater impact on the 412 acceleration of $\overline{F_{eddy}}$. When the acceleration of $\overline{F_{eddy}}$ is constant, the material with 413 higher σ/ρ corresponds to a smaller particle size. This indicates that the minimum 414 sortable particle size decreases with the increase of σ/ρ . Hence, improving the 415 416 conductivity of the material through low-temperature pretreatment or cooling after crushing [30] can reduce the minimum sortable particle size of ECS. Fig. 5 (b) is the 417 variation of the acceleration of $\overline{F_{eddy}}$ on Al particle with particle size under different 418 419 rotational speeds. It shows that there is also an interaction effect between the particle

size and the rotational speed of magnetic roller. When the particle size is close to the 420 optimal separation particle size, the influence of the rotational speed on the 421 acceleration of $\overline{F_{eddy}}$ is more significant, and the particle sizes corresponding to a 422 constant acceleration decrease with the increase of rotational speed. This indicates 423 that increasing the rotational speed of magnetic roller or the frequency of alternating 424 magnetic field can improve the separation efficiency of fine particles, which is 425 consistent with the application experience of ECS in industry [35]. Fig. 5(c) shows the 426 variation of the acceleration of $\overline{F_{eddy}}$ on Al particle with particle size under the two 427 428 magnetic pole arrangements of NNSS and NS when the rotational speed is 6000 rpm. It shows that the peak value of NNSS is on the right of the peak value of NS. This 429 indicates that NS is more suitable for separating fine particles, while NNSS has a 430 better separation effect for large particles. In the practical application of eddy current 431 separation technology, the non-uniform magnetic system combined with NNSS and 432 NS is a very common magnetic roller structure (see Fig. 1(b)). It turns out that the 433 non-uniform magnetic system can process mixtures with greater particle size 434 differences and greatly increase the separable particle size range of ECS. In addition, 435 the pole pitch of NNSS is twice that of NS, which is the essential difference between 436 the two magnetic pole arrangements. When dealing with fine particles, a magnetic 437 roller structure with a smaller pole pitch and a larger number of magnetic poles should 438 be selected. 439



Fig. 6. The influence of the interaction effects on the standard deviation of Lorentz force: (a) the variation of the standard deviation of the Lorentz force on Al and brass particles with particle size when the rotational speed is 6000 rpm; (b) the standard deviation of the Lorentz force on Al particle varies with particle size at different rotational speeds; (c) the variation of the standard deviation of the Lorentz force on Al particle varies with particle size at different rotational speeds; (c) the variation of the standard deviation of the Lorentz force on Al

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particle with particle size under the two magnetic pole arrangements at a rotational speed of 6000 rpm.

Fig. 6 shows the influence of the interaction effects between the particle size and 448 449 the material type, rotational speed and magnetic pole arrangement on the standard deviation of Lorentz force. It shows that the standard deviation of Lorentz force 450 increases with the increase of particle size under various experimental conditions, 451 452 indicating that large particle size will increase the randomness and distribution range of the falling points of non-ferrous metal particles. Fig. 5 (a) shows that the 453 acceleration difference of Lorentz force between different non-ferrous metals (such as 454 455 Al and brass) increases first and then decreases. Thus it can be deduced that with the increase of particle size, the average gap between the falling points of different 456 non-ferrous metal particles first increases and then decreases. Meanwhile, the 457 dispersion degree for the falling points of non-ferrous metal particles continues to 458 increase, so the separation efficiency between different non-ferrous metals may 459 increase slowly and then decrease sharply. Fig. 6 also shows that the dispersion 460 degree of the falling points of non-ferrous metal particles increases with the increase 461 in σ/ρ , rotational speed and pole pitch, which may have a negative impact on the 462 separation between different non-ferrous metals. Among them, the influence of 463 464 rotational speed is the weakest, and the influence of the magnetic roller structure is the most significant. The magnetic roller structure with a smaller pole pitch should be 465 considered when separating the mixtures of different non-ferrous metals. 466

467

3.3 The mechanism of particle size affecting separation



470 ms; (b) D=32 mm, t=18.8 ms; (c) D=1 mm, t=19.8 ms; (d) D=32 mm, t=19.8 ms; (e)

471 D=1 mm, t=20.8 ms; (f) D=32 mm, t=20.8 ms.

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472 To further clarify the internal mechanism of particle size affecting separation, it

is not enough to study the force on non-ferrous metal particles, and the 473 electromagnetic process inside particles can also provide important information. In 474 475 this regard, related research is mainly carried out through theoretical analysis. For example, a magnetic dipole model [32] was proposed based on theoretical derivation, 476 in which the Lorentz force ($F_{eddy} = m \cdot \nabla B$) on the non-ferrous metal particle mainly 477 depends on the magnetic moment (m) of the non-ferrous metal particle and the 478 magnetic field gradient (∇B). The magnetic moment is closely related to the eddy 479 current distribution in the non-ferrous metal particles. Therefore, the influence of 480 481 particle size on eddy current distribution and magnetic field gradient is investigated in this section. 482

Fig. 7 shows the eddy current distributions of Al particles with particle size of 1 483 484 mm and 32 mm at three different instants (18.8 ms, 19.8 ms and 20.8 ms) under a rotational speed of 1200 rpm. The three instants happen when the Al particle are 485 facing the NS junction, the middle of S pole and the SN junction on the magnetic 486 487 roller, respectively. It can be seen from Fig. 7 that the eddy current of 1 mm Al particles is more evenly distributed on the particle. The main flow of eddy current 488 circulates around the maximum cross-section of the particles, and the N pole and S 489 pole are located at two symmetrical ends on the particle, thus forming an analogue of 490 491 a magnetic dipole. The magnetic moment is determined by the following equation [33, 36]. 492

493
$$\mathbf{m} = \frac{1}{2} \int_{V} \mathbf{r} \times \mathbf{j} dV \tag{4}$$

494 where \mathbf{m} is the magnetic moment of the particle, \mathbf{r} is the coordinate vector with

respect to the centre of the mass particle, and **j** is the eddy current density in the 495 particle. According to the formula of the magnetic moment for a magnetic dipole, the 496 497 magnetic moment is proportional to the eddy current intensity and the area surrounded by the eddy current loop. Fig. 7 shows that the diameter and the eddy current intensity 498 of the 32 mm Al particle are one order of magnitude larger than that of the 1 mm Al 499 particle, so the Lorentz force generated in a larger non-ferrous metal particle is also 500 larger. In the range of small particle size, the eddy current intensity of the particle 501 increases with the increase of particle size, and the eddy current distribution is 502 503 uniform because the whole particle is contained in the effective area of magnetic field. In this case, the growth rate of Lorentz force is higher than that of particle mass with 504 the increase of particle size, and the acceleration of Lorentz force increases with the 505 506 particle size. When the particle size increases to a certain extent, the magnetic field intensity on each part of the particle is uneven due to the rapid attenuation of the 507 magnetic field near the surface of the magnetic roller. The part far away from the 508 magnetic roller on the particle exceeds the effective area of magnetic field, so the 509 eddy current is unequally distributed on the particle. Specifically, the main flow of 510 eddy current doesn't circulate around the maximum cross-section of the particle like 511 the case of the small size, but concentrates on the side close to the magnetic roller. 512 The N pole and S pole are also lean to this side, which leads to a smaller area 513 surrounded by the eddy current loop. And the magnetic moment of the electric current 514 loop with a smaller surrounding area is smaller. Thus, the growth rate of Lorentz force 515 will be less than that of particle mass if the particle size further increases. In this case, 516

the acceleration of Lorentz force gradually decreases, which has a negative impact on 517 the separation of large particles. In addition, the uneven distribution of the eddy 518 519 current in non-ferrous metal particles will further aggravate the instability of the Lorentz force, so the standard deviation of the Lorentz force increases greatly, which 520 521 brings difficulties to the separation between different non-ferrous metals. NNSS is significantly larger than NS in terms of the effective area of the magnetic field. This 522 study also compared the eddy current distribution of the Al particles under the two 523 magnetic pole arrangements of NNSS and NS to further verify the above reasons for 524 525 the uneven distribution of eddy current. The result is similar to the comparison of the eddy current distribution of particles with different sizes. The uneven distribution of 526 eddy current on the Al particles under NS magnetic system is more significant. In the 527 528 design and optimization process of ECS, the particle size range of the target material should be investigated first, and then ensure that the entire non-ferrous metal particle 529 is included in the effective area of the magnetic field. In this way, the problem of 530 531 uneven distribution of eddy current can be avoided.

To accurately evaluate the magnitude of the magnetic field gradient in the space where the non-ferrous metal particle is located, the volume integral of the magnetic field gradient inside the particle is used to quantify the magnetic field gradient intensity. The magnetic field gradient integral (∇B_{VI}) can be expressed by the following formula.

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$$\nabla \mathbf{B}_{VI} = \iiint \nabla \mathbf{B}(\mathbf{x}, \mathbf{y}, \mathbf{z}) dV \tag{5}$$

538 where $\nabla B(x, y, z)$ is the magnetic field gradient at position (x, y, z). Fig. 8 is the

variation of the time-average of the magnetic field gradient integration in the 539 non-ferrous metal particle with particle size. It shows that the magnetic field gradient 540 541 in the region occupied by the particle increases with the increase of particle size. The results in Fig. 7 and Fig. 8 show that with the decrease of particle size, the magnetic 542 gradient in the particle and the magnetic moment formed by eddy current will 543 decrease significantly, resulting in the rapid reduction of the Lorentz force on the 544 non-ferrous metal particle, and the power relationship between the Lorentz force and 545 particle size is higher than the cubic relationship between mass and particle size (m =546 $\rho \cdot \frac{4}{3}\pi r^3$). Although fine particles can be completely contained in the effective area of 547 the magnetic field, and the main flow of eddy current in fine particles can circulate the 548 maximum cross-section of particles. Still, the reduction speed of the Lorentz force is 549 550 higher than that of particle mass when the particle size decreases. Therefore, the acceleration of Lorentz force gradually decreases, and gravity, aerodynamic drag 551 force [37], etc. gradually occupy a dominant position in determining the particle 552 trajectory, which causes the problem of difficult separation of fine particles. Based on 553 the above analysis of large and fine particles, it can better explain why there is an 554 optimal particle size for a specific eddy current separator. The results also indicate 555 that the magnetic field gradient in the spatial region of the target mixture should be 556 557 enhanced as much as possible in the design and optimization of the magnetic roller.



559 Fig. 8. The variation of the time-average of the magnetic field gradient integration in

the non-ferrous metal particle with particle size.

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562 The influence rule of the particle size on the eddy current separation, and the 563 mechanisms involved, are of critical importance for the efficient utilization of ECS

4. Conclusion

technology in various mixtures. These issues were studied by combining the numerical simulations and the separation experiments. The correlation coefficients between the physical quantities in the simulations and the performance indexes from the separation experiments are all greater than 0.94. This further validates the three-dimensional transient simulation model of ECS used. The main conclusions can be summarized as follow:

570 (1) With the decrease of particle size, the translational motion of non-ferrous 571 metal particles increases first and then decreases rapidly, while the rotational motion 572 continues to increase. To improve the separation efficiency of fine particles, the 573 rotational speed and the σ/ρ should be increased, the pole pitch should be reduced, and the rotational motion of the particles should be utilized efficiently.

575 (2) The particle size determines separation efficiency by affecting the magnitude 576 and distribution uniformity of eddy currents. When designing and optimizing the ECS, 577 the particle size range of the target mixture should be investigated in advance, and the 578 particles should be within the effective area of the magnetic field. Meanwhile, the 579 magnetic field gradient of the space region occupied by the particles should be 580 increased as much as possible.

581 These results can provide guidance for the design and optimization of ECS for 582 fine particles such as the electronic waste and the incineration bottom ash, which may 583 also expand the new application areas for this green technology.

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